Glacio-isostatic adjustment in Fennoscandia revisited

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Abstract. The theory of load-induced relaxation of the layered Maxwell half-space is applied to the study of glacio-isostatic adjustment in Fennoscandia. The interpretation uses emergence data from Ångermanland (Sweden) and uplift-rate data from the Gulf of Bothnia. With mantle viscosity fixed at $10^{21}$ Pa s, the data can be explained by an earth model characterized by (a) an elastic surface layer of conventional thickness (about 100 km) superimposed on a low-viscosity layer or (b) an elastic surface layer of enhanced thickness (about 200 km) and no low-viscosity layer. Reasons for this ambiguity and possible ways to resolve it in future studies are suggested. The investigation also attempts to interpret the negative free-air gravity anomaly observed over the deglaciated region of Fennoscandia. Either (i) enhanced mantle viscosity below 670 km depth or (ii) a transition zone in viscosity between an elastic surface layer and a viscous mantle is required to predict negative anomalies substantially larger than 3 mgal.

Key words: Fennoscandia – Isostasy – Maxwell continuum

Introduction

More than 50 years ago, Reginald Daly drew attention to post-glacial uplift and discussed two rheological earth models, which he designated “bulge hypothesis” and “punching hypothesis” (Daly, 1934, pp. 120–126).

The bulge hypothesis assumes that flow is restricted to a near-surface layer (channel model). Mass conservation then requires the existence of a substantial peripheral bulge during glaciation. During and after deglaciation, the central depression is elevated to equilibrium while the bulge collapses.

Daly believed that geological evidence in support of a peripheral bulge is missing in Fennoscandia and North America. He therefore suggested that the glacial load had been punched through the elastic crust, forcing flow to great depths (deep-flow model). A distinctive feature of this model is that, with deglaciation, both central and peripheral regions are initially uplifted sympathetically. The later stages of readjustment include crustal failure and a reversal of the upward movement in the periphery (Daly, 1934, Fig. 70).

The following year, Haskell (1935) demonstrated quantitatively that the main features of Daly’s punching hypothesis are also produced by a uniform, Newtonian viscous half-space. Haskell also interpreted the Fennoscandian uplift with this model. His estimate of the dynamic mantle viscosity was about $10^{21}$ Pa s. An essential ingredient of Haskell’s analysis was the assumption of a residual depression of 20 m near the glaciation centre, corresponding to a free-air gravity anomaly of approximately $-3$ mgal.

The question of the causal relation between the observed gravity anomaly and the Pleistocene glaciation in Fennoscandia has been discussed since Haskell’s pioneer study (summarized by Cathles, 1975, pp. 151–154; Balling, 1980). The difficulties in interpreting the gravity field are related to the fact that, although negative anomalies predominate in Fennoscandia, the gravity pattern is irregular. In particular, there is no pronounced correlation with the topography of the Pleistocene ice-sheet. Therefore, differing values for the remaining uplift can be inferred from the free-air gravity data.

Niskanen (1939), for example, suggested that the deglaciation-induced portion has a peak value of about $-30$ mgal, giving a residual depression of about 200 m. This led several investigators to dismiss Haskell’s deep-flow model and use various kinds of channel model, which produce enhanced residual depressions. The quantitative development of channel models was initiated by van Bemmelen and Berlage (1935) and subsequently extended by many other investigators (summarized by Cathles, 1980; Walcott, 1980). Since there is now evidence for an almost uniformly viscous mantle (Cathles, 1975; Peltier and Andrews, 1976; Wu and Peltier, 1983), channel models have fallen into disrepute.

Recently, Balling (1980) attempted to substantiate previous claims of more moderate deglaciation-induced anomalies (e.g. Walcott, 1973). After filtering out a non-glacial component believed to be related to the structure of the earth’s crust and upper mantle, Balling inferred a glacial component of about $-17$ mgal for central Fennoscandia (Fig. 1). This value implies that the positive anomalies in the peripheral region reflect a superimposed long-wavelength geoid high. However, deglaciation-induced anomalies of this order are still substantial and, as Haskell’s (1935) and Cathles’ (1975) work shows, incompatible with simple deep-flow models.

A possible way out of this impasse was proposed by Anderson (1984). Using statistical analysis, he suggested...
that the observed geoid low over Fennoscandia is caused predominantly by an approximately twofold increase in crustal thickness from the Norwegian Sea and northern Germany toward central Fennoscandia. Anderson therefore concluded that contributions to the geoid anomaly associated with crustal structure are much more substantial than generally assumed. If this is true, the glacial component of the gravity anomaly must be quite small and can be easily explained with simple deep-flow models.

An alternative way to reconcile gravity observations with gravity predictions was discussed by Peltier and Wu (1982). Using Maxwell earth models, of essentially uniform viscosity and with the same density and elastic structure as seismic earth model 1066B (Gilbert and Dziewonski, 1975), Peltier and Wu predicted free-air gravity anomalies of about -20 mgal for Fennoscandia. The increase in magnitude was largely a consequence of treating the entire density structure of model 1066B as non-adiabatic.

It has also been suggested that an elastic surface layer (lithosphere) is actively involved in the isostatic adjustment process in Fennoscandia. One of the modern investigators who devoted explicit attention to the lithosphere was McConnell (1968), who interpreted relaxation-time estimates from a spectral decomposition of strandline data from Fennoscandia. He used a layered, Newtonian viscous half-space model and proposed a lithospheric thickness of 120 km.

Cathles’ study of glacio-isostatic adjustment was biased by his idea that the Fennoscandian uplift is insensitive to the presence of the lithosphere (Cathles, 1975, p. 153). In his flat-earth analysis, he arbitrarily adopted a lithosphere of about 70 km thickness (Cathles, 1975, pp. 184-191). Recent results (Wolf, 1984, 1985a) showed that this is probably a misconception.

In the light of these inconsistencies, the present study re-interprets glacio-isostatic adjustment in Fennoscandia, based on the theory of the layered, incompressible Maxwell half-space. The complex Fennoscandian deglaciation history is simulated by several simplified models. Particular attention is paid to the question of lithospheric thickness. The results will show that, although the adjustment data used are compatible with a lithosphere of about 200 km thickness below Fennoscandia, the data cannot be construed to require this value.

Further, the seismic discontinuity at 670 km depth is discussed in relation to the free-air gravity anomaly over Fennoscandia. According to the preliminary reference earth model (PREM; Dziewonski and Anderson, 1981), this discontinuity is characterized by a density increase of 390 kg m$^{-3}$, which is treated as non-adiabatic in the present study. Although the gravity predictions are largely insensitive to this density contrast, results will show that they are very sensitive to the value adopted for the viscosity below 670 km depth. The study also proposes an alternative explanation of the gravity anomaly, suggesting that it is related to the relaxation of a transition zone in viscosity between the elastic surface layer and the mantle.

**Theoretical model**

The rheological model basic to this interpretation is the layered, incompressible Maxwell half-space. Each of its
layers is characterized by four parameters: thickness $h$, density $\rho$, rigidity $\mu$ and viscosity $\eta$. The response of this model to surface loads was analysed and discussed previously (Wolf, 1985a).

The glaciation of Fennoscandia (Fig. 2a) is modelled as a Heaviside unloading event at 11 ka B.P. (Fig. 2b, Table 1, load model 1) and as a stepwise-discontinuous loading history (Fig. 2c, Table 1, load model 2). Load model 1 is the first approximation. It simulates the fast decay of the Fennoscandian ice-sheet following a period of stagnation between 12 and 10 ka B.P. Load model 2 is more realistic, although several important features of the Fennoscandian glaciation are unknown, for example, the extent of the ice-sheet in the shelf regions of the Norwegian and Barents Seas. However, the location of the uplift site employed in this study in Ångermanland (Sweden) (Fig. 2) is very close to the Pleistocene glaciation centre and therefore largely insensitive to complications near the ice margin.

Load model 1 can only be used with earth models that have short relaxation times (Table 2, earth models A.1 and L.1). For simplicity, the cross-section of the load is assumed to be rectangular and the load radius to be fixed during load cycles 1–19. During each of these cycles the load thickness increases according to $h_0(t-t_N)/(t_{N+1}-t_N)$, where $t_N$ is the beginning of the $N$-th load cycle and $t_{N+1}<t<t_{N+2}$. The maximum thickness $h_0$ reached at the end of each cycle is determined by the ratio $h_0/R$ adopted for load cycle 20. The load density is always assumed to be 1000 kg m$^{-3}$.

### Data analysis and discussion

The emergence data from Ångermanland are of prime importance to this interpretation. The data set is based on a series of raised beaches, whose ages are constrained by varve sequences. The data were originally published by Lindén (1938), but can also be found elsewhere (e.g. Lliboutry, 1971; Cathles, 1975, p. 196). Since the dating of the strandlines is based on varve chronology, the relative ages of the Ångermanland strandline series are very accurate.

The observed emergence of a strandline is controlled by uplift of the earth’s surface and by changes in sea level. Sea-level changes are related to (a) influx of melted ice and (b) geoid perturbations produced by redistribution of water and by simultaneous redistribution of mantle material. Contribution (a) has been named eustatic change. This has a clear meaning only if it is defined as the ocean-wide average change in mean sea level (Walcott, 1972). Contribution (b) depends on location but can become as large as contribution (a) (Farrell and Clark, 1976; Clark et al., 1978; Peltier et al., 1978).

Near major glaciation centres, sea-level changes have been small compared with surface uplift after about 10 ka B.P. Before that, the lowering of eustatic sea level was partially counterbalanced by the rise of the geoid below the melting ice mass (Wu and Peltier, 1983, Fig. 4a). The portion of the emergence of old strandlines caused by uplift
of the earth's surface may therefore be approximately bracketed by the observed emergence and this emergence corrected for eustatic sea-level rise.

The following uplift diagrams symbolize this range by vertical bars, where corrections for eustatic sea-level change according to Fairbridge (1961, Fig. 8) have been applied. The observed uplift during the time interval [t,0] can now be compared with the predicted uplift \( H(t) = w(t) + w(0) \), where \( w \) is the (downward) surface displacement for the model under consideration and \( t = 0 \) is present time.

The study of the Fennoscandinavian uplift begins by using load model 1. The observed uplift in Ångermanland is compared with the theoretical uplift for two distinct earth models, both of which use a mantle viscosity of \( 10^{21} \) Pa s.

Figure 3a shows an interpretation similar to that proposed by Cathles (1975, pp. 184–191), with a load thickness of 1.50 km. The earth model uses a lithosphere of conventional thickness (100 km) underlain by a low-viscosity layer (asthenosphere) (Table 2, earth model A.1). If the viscosity of the asthenosphere is selected properly, a satisfactory fit of the data is achieved.

Figure 3b proposes an alternative interpretation of the same data set. The load thickness has been increased to 1.90 km, and the Earth model has a lithosphere but no asthenosphere (Table 2, earth model L.1). This time the data are bracketed by the curves for enhanced lithospheric thicknesses of 170 km and 230 km.

If the load thickness is further increased, the observations are compatible with even larger lithospheric thicknesses. Conversely, the fit produced in Fig. 3a is a consequence of the reduced load thickness that is used. This behaviour is consistent with results by Wolf (1985a, Figs. 10a and 11a). The ambiguous interpretation is therefore partly a consequence of a trade-off between lithospheric thickness and load thickness.

The next step is to use earth model L.1 with load model 2. For lithospheric thicknesses of about 200 km, this requires \( h_0^2 / R = 4.0 \times 10^{-3} \) km. As Fig. 4a shows, the fit of the uplift data is similar to that in Fig. 3b. Closer inspection of Fig. 4a reveals, however, that younger beaches are consistent with a lithosphere slightly thinner than 200 km, whereas older beaches are better explained if the lithosphere is somewhat thicker.

Figure 4b shows the observed uplift rates (e.g. Balling, 1980) on a north-south profile in the Gulf of Bothnia (Fig. 2c) as stippled band and the theoretical uplift rates for the same model parameters. The uplift rates are obviously very sensitive to lithospheric thickness. Similarly to Fig. 4a, a thickness of approximately 170 km produces the best fit.

As expected, the theoretical models discussed so far have small free-air gravity anomalies. For the 200 km thick lithosphere, the peak value is approximately −4 mgal, giving a residual depression of about 28 m. If Balling's (1980) filtered anomaly (Fig. 1) represents the deglaciation-induced portion of the gravity field in Fennoscandia, this interpretation appears untenable.

The study therefore investigates the effects of a contrast in viscosity or density at 670 km depth (Table 2, earth model M.4). The modifications apply to a saw-tooth loading history (Fig. 5) and are shown in Fig. 6. The radius of 1000 km for the rectangular load is selected to represent conditions during the last glacial maximum at about 18 ka B.P. The sensitivity of the response to lower-mantle viscosity is obvious. At time \( t = 12 \) ka, the residual surface depression is increased threefold for a twofold increase in lower-mantle viscosity. The modifications produced by the internal density contrast are much smaller in comparison.

Figure 7 interprets the Ångermanland uplift data using
Fig. 5. Saw-tooth loading history applicable to Figs. 6, 9 and 11

Fig. 6. Vertical surface displacement $w$ as function of axial distance $r$ for several times (in units of ka) after load removal; predictions apply to saw-tooth loading history (Fig. 5) with $R = 1000$ km and earth model M.4 with $h_1 = 200$ km and $\rho_3\rho_2 = 0$, $\eta_3 = 1.0 \times 10^{21}$ Pa s (solid), $\rho_3\rho_2 = 0$, $\eta_3 = 2.0 \times 10^{21}$ Pa s (dashed) or $\rho_3\rho_2 = 390$ kg m$^{-3}$, $\eta_3 = 2.0 \times 10^{21}$ Pa s (dotted)

Fig. 7a and b. As for Fig. 4 except that predictions apply to load model 2 with $h_0/R = 3.0 \times 10^{-3}$ km and earth model M.4 with $\rho_3\rho_2 = 390$ kg m$^{-3}$, $\eta_3 = 2.0 \times 10^{21}$ Pa s and $h_1 = 170$ km (dashed), $h_1 = 200$ km (dot-dashed) or $h_1 = 230$ km (dotted); associated free-air gravity prediction at $r=0$, $t=0$ is $\Delta g = -9.4$ mgal (dashed), $\Delta g = -7.7$ mgal (dot-dashed) or $\Delta g = -6.4$ mgal (dotted)

Fig. 8. Viscosity $\eta$ as function of depth $z$ for $Q \to \infty$ (solid), $Q = 500$ kJ mol$^{-1}$ (dashed) or $Q = 200$ kJ mol$^{-1}$ (dotted); continuous functions are approximated by three uniform layers

Fig. 9. As for Fig. 6 except that predictions apply to saw-tooth loading history (Fig. 5) with $R = 600$ km and earth model L.1 with $h_1 = 200$ km (solid), earth model L.4 (dashed) or earth model L.5 (dotted)

this earth model. Compared with the model used for Fig. 4, the viscosity below 670 km is higher by a factor of two and the density is increased by $390$ kg m$^{-3}$ in this depth range. As before, results apply to load model 2. During load cycles 1–19, $R = 1000$ km; during load cycle 20, $h_0/R = 3.0 \times 10^{-3}$ km. The reduction in load thickness, compared with Fig. 4, is required to predict the correct present-day uplift rates. The fit of the uplift and uplift-rate data is comparable to Fig. 4, but the theoretical free-air gravity anomaly is enhanced significantly ($\Delta g = -7.7$ mgal for $h_1 = 200$ km).

In order to predict a value near $-17$ mgal, either additional internal buoyancy or a further increase in lower-mantle viscosity is required. Neither alternative appears practicable, however. Whereas the former hinges on the assumption that each additional density discontinuity is modelled as a non-adiabatic increase, the latter renders a satisfactory fit of the uplift and uplift-rate data increasingly difficult.

An alternative mechanism for enhancing gravity predictions is provided by the introduction of a transition zone in viscosity between the elastic surface layer and the viscous mantle. For example, assuming a linear geotherm which passes through points $T = 0^\circ$ C, $z = 0$ km and $T = 1400^\circ$ C, $z = 200$ km (Jordan, 1981), the temperature distribution can be converted into a viscosity distribution, provided that the viscosity $\eta$ at depth $z = 200$ km and the activation energy $Q$ in the depth range $0 \leq z \leq 200$ km are known (details in Wolf, 1985a).

Figure 8 uses a mantle viscosity of $10^{21}$ Pa s and shows viscosity-depth distributions for three activation energies. For computational ease, the continuous distributions are approximated by three uniform layers, which constitute the thermal lithosphere (Table 2, earth models L.4 and L.5). The portion which responds elastically is called the mechanical lithosphere. If the loading time is sufficiently short or if the activation energy is sufficiently high, the "mechanical thickness" approaches the "thermald thickness".

The modifications of the response produced by a transition zone in viscosity are shown in Fig. 9 for earth models L.1, L.4 and L.5. As for Fig. 6, results apply to a saw-tooth loading history (Fig. 5). However, the radius of the rectan-
the viscosity stratification of the lithosphere. The opposite
expected. theoretical uplift proves essentially insensitive to
km. The fit is optimized for earth model L.5, but as ex­
retical curves apply to load model 2. During load cycles
uplift-rate predictions for the same earth models. The theo­
is, however, two- to threefold larger compared with the
model without transition zone.
Therefore, predictions of
information produced by the cyclic loading is not appreciable.
(Wolf, 1985a, Fig. 7), the initial decay of the excess defor­
mation produced by the cyclic loading is not appreciable.
and earth model L.5 (dashed), earth model L.4 (dot-dashed) or earth model L.1 with \( h_1 = 200 \) km (dotted); associated free-air gravity prediction at \( r = 0, t = 0 \) is \( \Delta g = -10.9 \text{ mgal} \) (dashed), \( \Delta g = -7.5 \text{ mgal} \) (dot-dashed) or \( \Delta g = -3.5 \text{ mgal} \) (dotted)

Fig. 11. Free-air gravity prediction \( \Delta g \) at \( r = 0, t = 12 \text{ ka} \) as function of load radius \( R \); predictions apply to saw-tooth loading history (Fig. 5) and earth model L.1 with \( h_1 = 200 \) km (solid), earth model M.4 with \( h_1 = 200 \) km, \( \rho_3 - \rho_2 = 390 \text{ kg m}^{-3} \) and \( \eta_3 = 2.0 \times 10^{21} \text{ Pa s} \) (dashed) or earth model L.5 (dotted); cross-hatched band indicates glacial component of gravity anomaly (Fig. 1)

angular load is reduced to 600 km. Because of the long relaxa­
tion times of the modes supported by the transition zone
(Wolf, 1985a, Fig. 7), the initial decay of the excess deform­
amon produced by the cyclic loading is not appreciable.
Therefore, predictions of relative uplift are nearly una­
fected. The absolute value of the surface depression at time
\( t = 12 \text{ ka} \), and thus the theoretical free-air gravity anomaly, is, however, two- to threefold larger compared with the model without transition zone.

This is substantiated by Fig. 10, which shows uplift and uplift-rate predictions for the same earth models. The theo­
etrical curves apply to load model 2. During load cycles 1–19, \( R = 600 \text{ km} \); during load cycle 20, \( h_0^2/R = 3.0 \times 10^{-3} \) km. The fit is optimized for earth model L.5, but, as ex­
pected, theoretical uplift proves essentially insensitive to
the viscosity stratification of the lithosphere. The opposite
holds for free-air gravity. For earth model L.5, peak values of \(-11 \text{ mgal} \) are predicted.

By intuitive reasoning, the importance of lithospheric
relaxation is expected to depend on the ratio between load
radius and lithospheric thickness. If this ratio is large, the
lithosphere is virtually “transparent”; conditions close to
local compensation apply, and the response should be in­
sensitive to lithospheric relaxation.

This is illustrated in Fig. 11, which, for the saw-tooth
loading history (Fig. 5), shows gravity predictions for rect­
angular loads of different radii. Comparison of the anom­
lies for earth models L.1 and L.5 shows that lithospheric
relaxation becomes insignificant if the load radius exceeds
about 700–800 km [see Wolf (1985a, Fig. 13) for a different example]. Loads of larger radii are, however, sensitive to
lower-mantle viscosity and to internal buoyancy associated
with the density contrast at 670 km depth, as shown for
earth model M.4. For comparison, Fig. 11 also shows fil­
tered peak gravity values according to Balling (1980) (with­
out corrections for the long-wavelength geoid high).

Conclusion
The main conclusion of this study is that uplift data from
Angermanland and uplift-rate data from a profile in the
Gulf of Bothnia are insufficient to constrain lithospheric
thickness in Fennoscandia. The study has placed special
emphasis on earth models with a lithosphere of about
200 km thickness and shown that these models are compati­
bles with the two data sets. In a previous investigation, a
lithosphere of about 70 km thickness was adopted, and a
comparable fit of the data sets used here was achieved
(Cathles, 1975, pp. 184–191).

A characteristic feature of interpretations that use earth
models with a thin lithosphere appears to be that an astheno­
sphere is required below the lithosphere. Various model
calculations have shown that the presence of an astheno­
sphere controls the movement of the zero-crossings separ­
ing the downwarped central region from the upwarped pe­
eripheral region. If mantle viscosity is uniform, the zero­
crossings move inward after deglaciation. The presence of
an asthenosphere leads, however, to stationary zero-cross­
ings or even reverses the direction (e.g. Cathles, 1975, Figs.
IV-28 and IV-29). At present, opinions differ on the move­
ment of the zero-crossings in Fennoscandia (e.g. Cathles,
1980; Mörner, 1980). This feature therefore cannot be em­
ployed yet as circumstantial evidence for the thickness of
the lithosphere.

More promising for this purpose are the delevelled
strandlines associated with pro- or post-glacial lakes or seas.
If the strandlines are sufficiently old, their tilts are sensitive
to lithospheric thickness. Pro-glacial-lake tilts were used to
constrain lithospheric thickness in North America (Wal­
cott, 1970; Wolf, 1985b, 1986). The interpretations fa­
voured a thickness of less than 100 km, which is lower than
Peltier’s (1984) estimate of about 200 km based on relative
sea-level data from the North American east coast. In Fen­
noscandia, a complete sequence of strandlines has been
mapped and dated (e.g. Donner, 1980; Eronen, 1983). The
oldest of these strandlines was formed at approximately
10 ka B.P. It is therefore pro-glacial, and its tilt is expected
to be sensitive to lithospheric thickness. A careful analysis
of strandline tilt may therefore help resolve the ambiguity
in the interpretation.
The second aspect of this study has been the investigation of mechanisms which are capable of enhancing the gravity predictions without sacrificing the fit of the uplift data. Peltier and Wu (1982) achieved this largely by allowing sufficient internal buoyancy. The present study has restricted internal buoyancy to the density contrast at 670 km depth, in order to display more clearly the effect of lower-mantle viscosity on the gravity predictions. Alternatively, a transition zone in viscosity has been invoked to enhance the gravity anomaly. Either modification allows the prediction of negative anomalies of up to 11 mgal. This is rather small compared with the value proposed by Balling (1980) for the glacial component of the Fennoscandian gravity anomaly. Conversely, it is large in view of Anderson's (1984) study, which implies that the glacial component is minor.

Whether the Fennoscandian gravity data can constrain the earth's viscosity structure therefore depends on accurate determination of the size of the non-glacial component of the anomaly. Until this problem has been solved, studies of the kind discussed here mainly serve to demonstrate that interpretations using deep-flow models do not fail automatically if the glacial component turns out to be large.

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