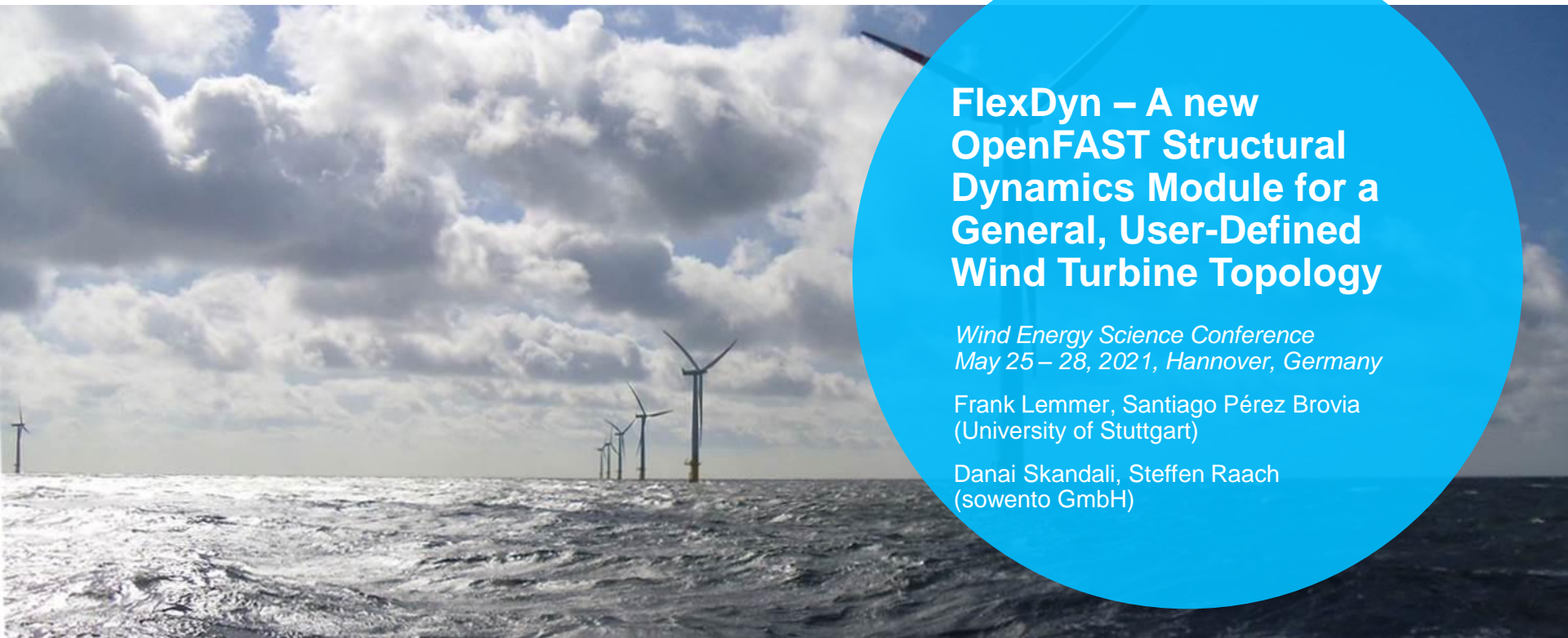


**University of Stuttgart**  
Stuttgart Wind Energy (SWE)  
@ Institute of Aircraft Design



## FlexDyn – A new OpenFAST Structural Dynamics Module for a General, User-Defined Wind Turbine Topology

*Wind Energy Science Conference  
May 25 – 28, 2021, Hannover, Germany*

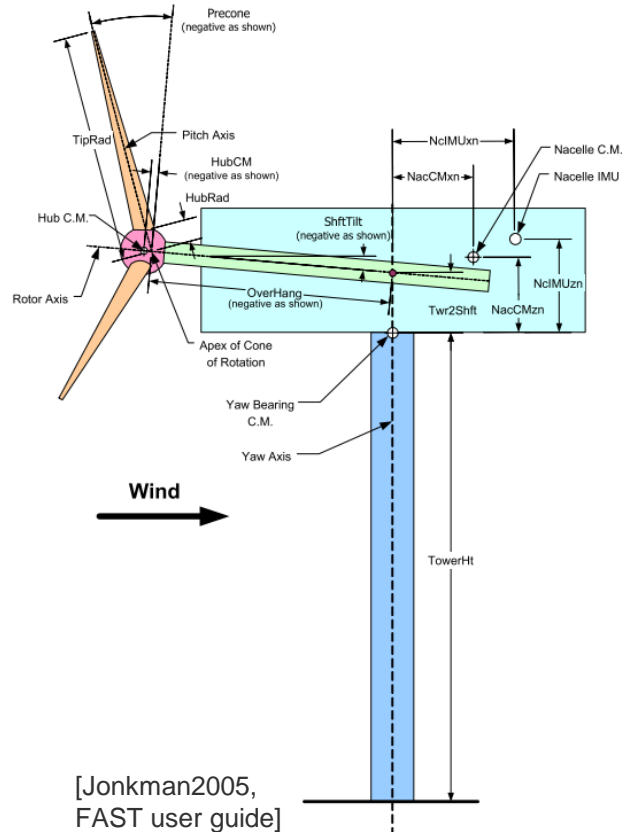
Frank Lemmer, Santiago Pérez Brovia  
(University of Stuttgart)

Danai Skandali, Steffen Raach  
(sowento GmbH)



# Background: Aero-Hydro-Servo-Elastic Modeling

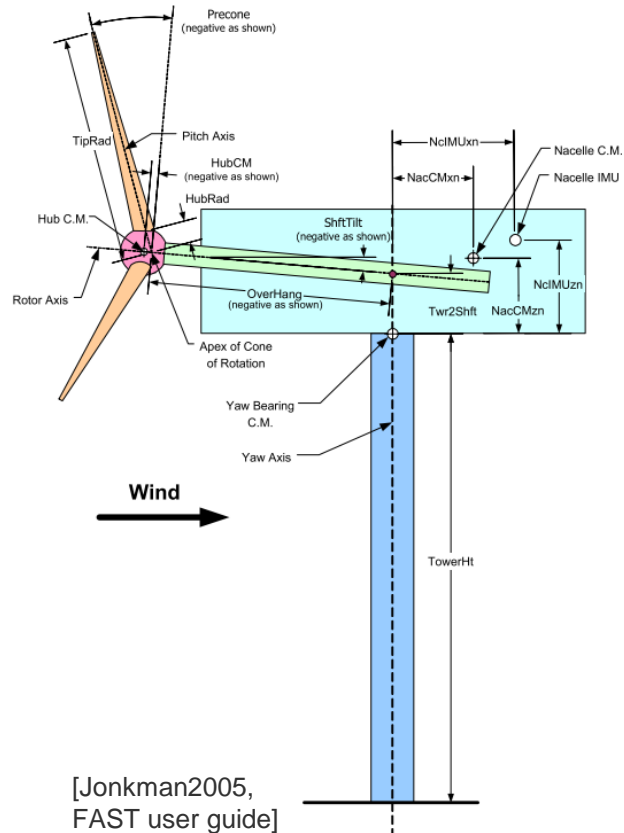
- Structural dynamics, aerodynamics, hydrodynamics, controls



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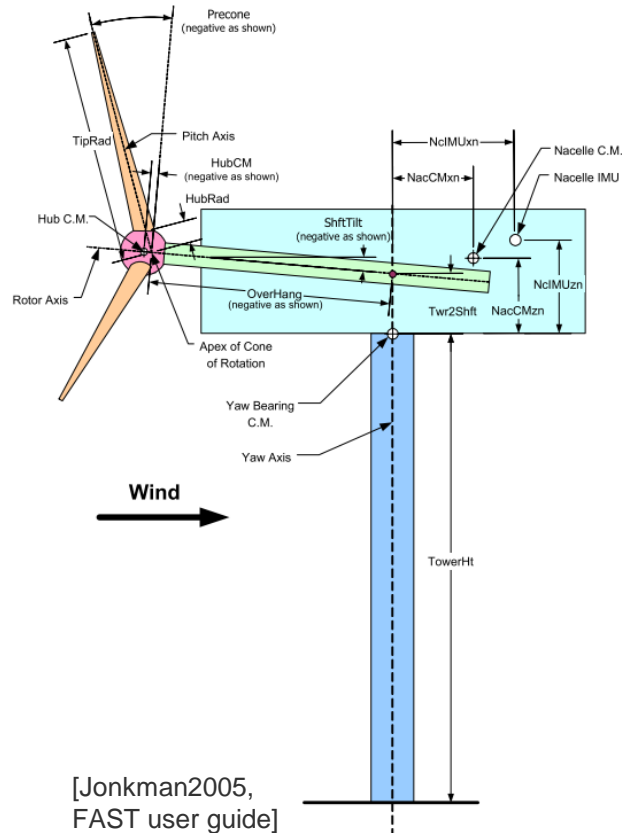
- Nonlinear time-domain
- Linearization



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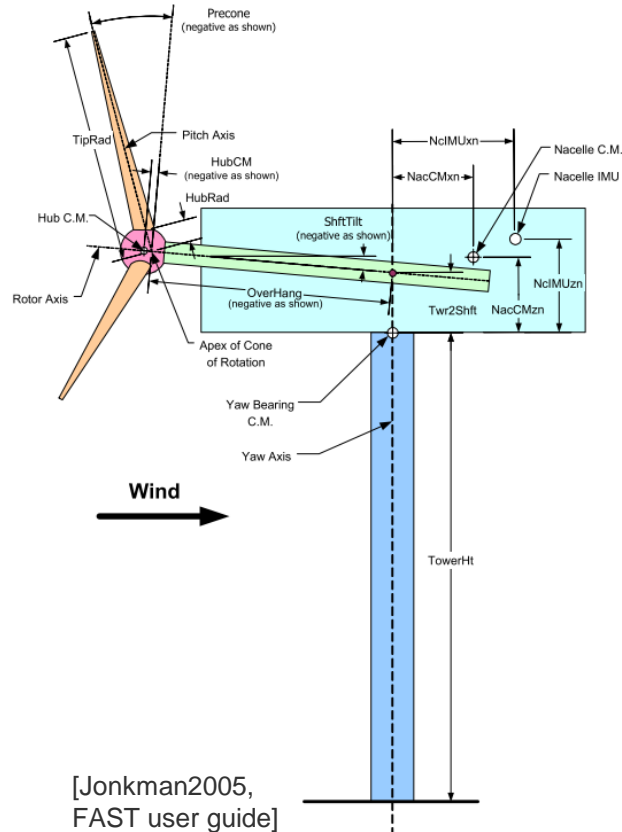


- „Engineering“ model
- Blade-element momentum theory
- „Modal“ reduction of beams

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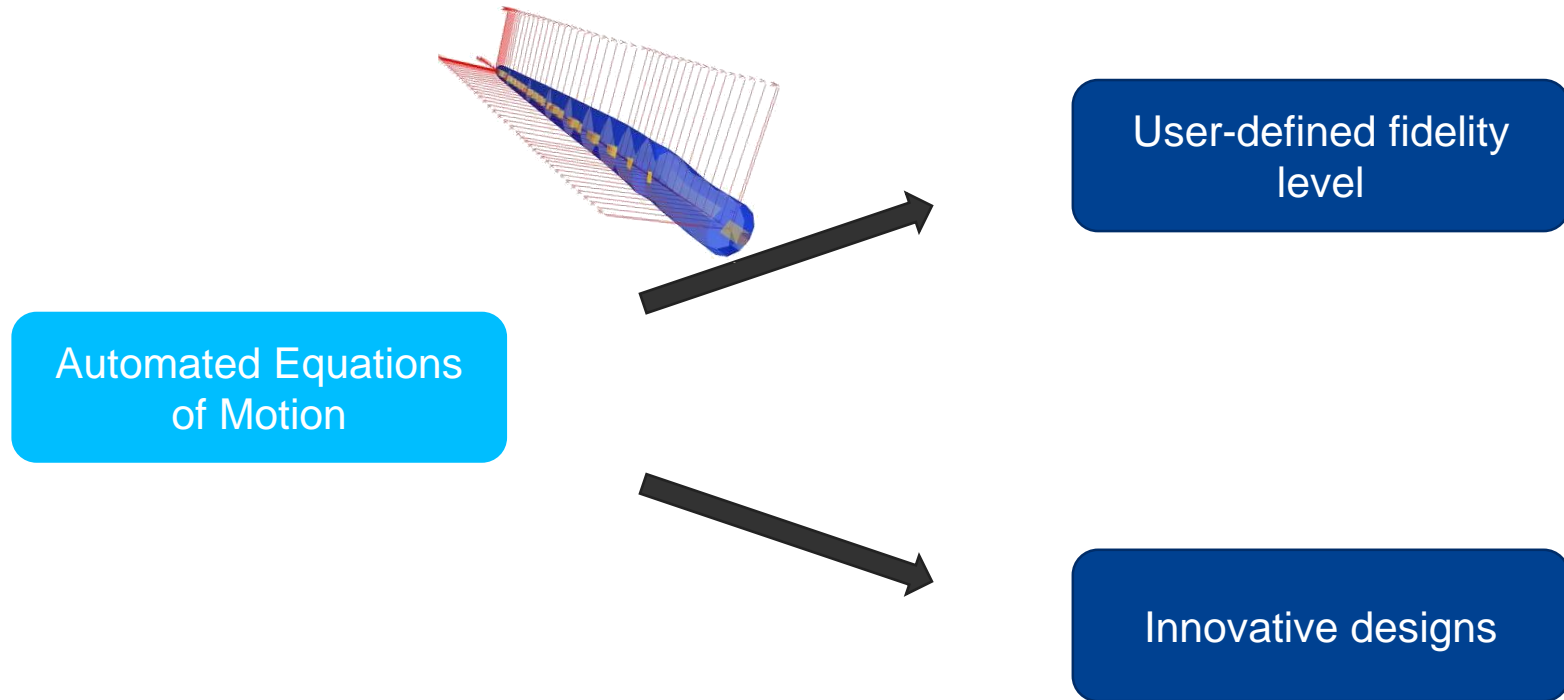
- Nonlinear time-domain
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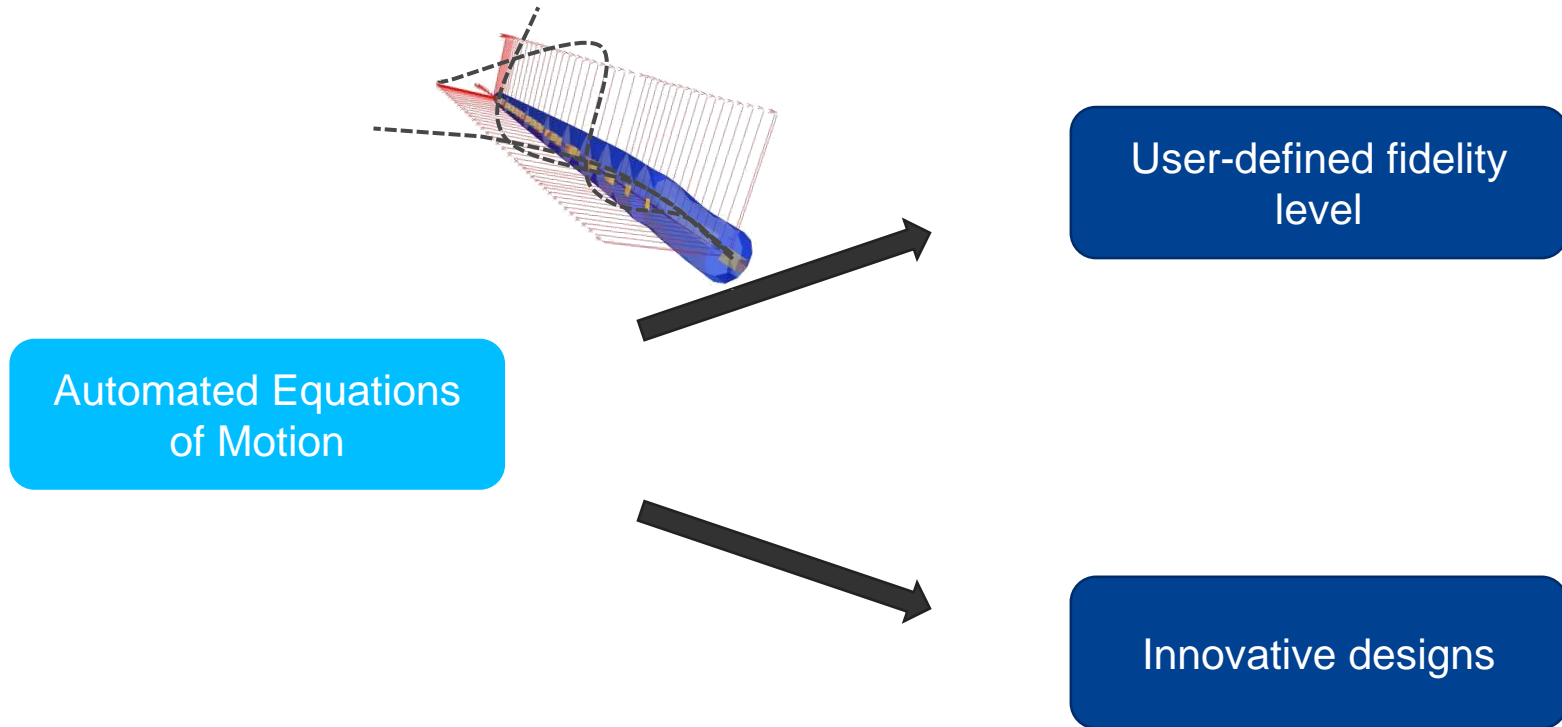
- „Engineering“ model
- Blade-element momentum theory
- „Modal“ reduction of beams

- Two/three bladed
- Upwind/downwind
- Onshore/Offshore

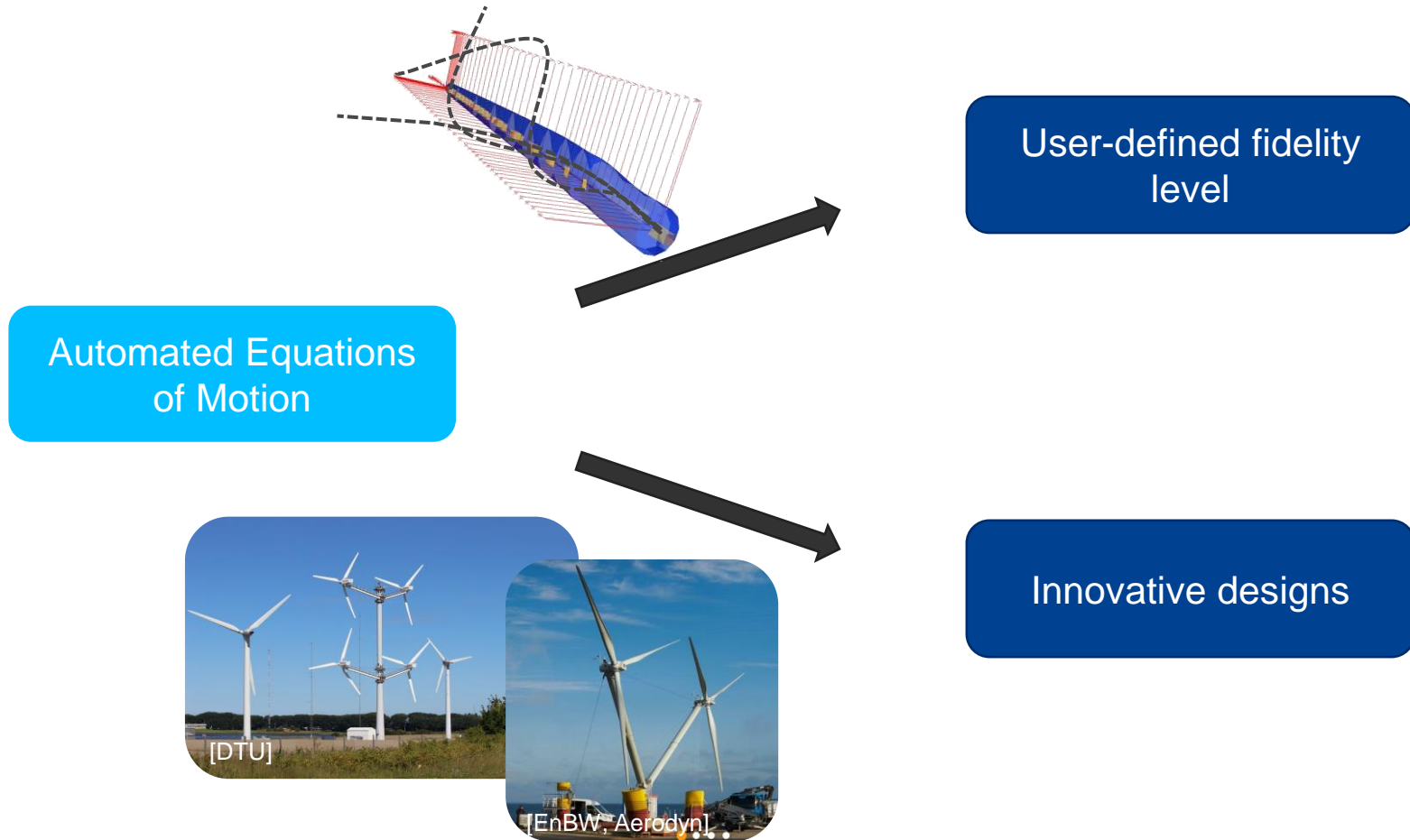
# Motivation: User-Defined Multibody System Topology



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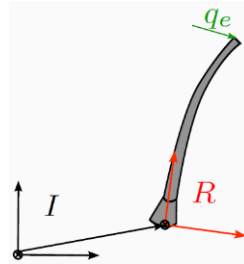




# Methodology: Newton-Euler Formalism

## 1. Topology definition:

- Reference frame position, angular velocity
- Distributed mass, elasticity

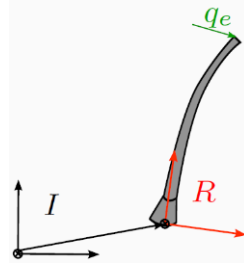


Automated Equations  
of Motion

# Methodology: Newton-Euler Formalism

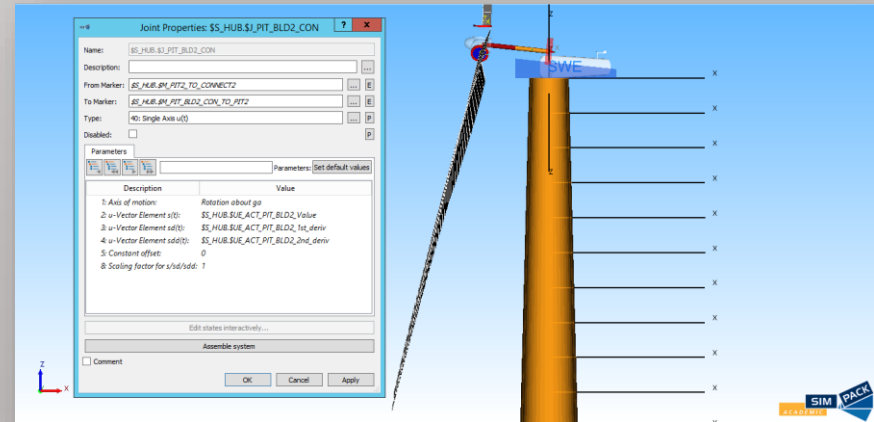
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Automated Equations of Motion

## Example from Simpack:

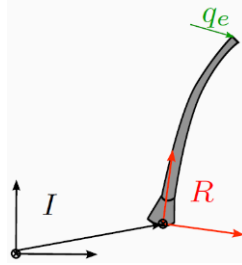


Schiehlen, W., & Eberhard, P. (2014). *Applied Dynamics* (1st ed.). <https://doi.org/10.1007/978-3-319-07335-4>

# Methodology: Newton-Euler Formalism

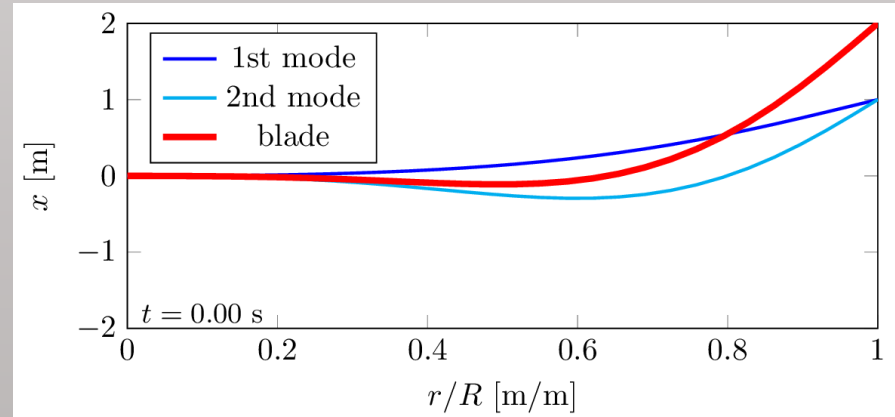
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Automated Equations  
of Motion

Shape functions (by David Schlipf, WETI, HS Flensburg):

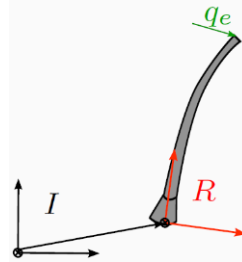


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# Methodology: Newton-Euler Formalism

## 1. Topology definition:

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## 2. Newton-Euler Formalism

$$\underbrace{M\ddot{z}} + h_\omega = h_g + h_d + h_e + h_r$$

$$M\ddot{z} = \begin{bmatrix} m & & sym. \\ m\tilde{S}(c) & I & \\ C_t & C_r & M_e \end{bmatrix} \begin{bmatrix} {}^R a \\ {}^R \alpha \\ \ddot{q}_e \end{bmatrix}$$

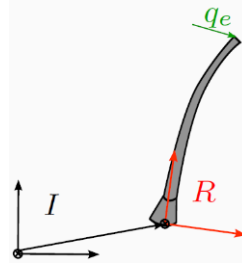
body  $i$

Automated Equations  
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Automated Equations of Motion

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Transformation

$$J = [J_{t,1}, J_{r,1}, J_{e,1}, \dots, J_{t,p}, J_{r,p}, J_{e,p}]^T$$

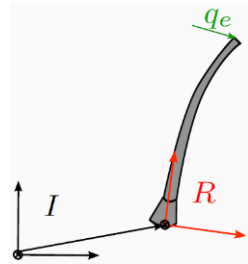
## 3. Minimal coordinates

$$\bar{M}(q)\ddot{q} + \bar{h}_\omega(q, \dot{q}) = \bar{h}_g(q) + \bar{h}_d(q, \dot{q}) + \bar{h}_e(q_e)$$

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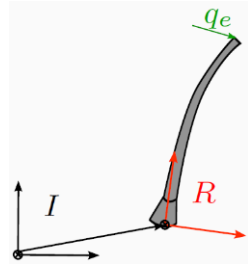
$$q = [x_p, z_p, \beta_p, \varphi, x_t, \dots]^T$$

Automated Equations  
of Motion

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Automated Equations of Motion

body  $i$

Transformation

$$J = [J_{t,1}, J_{r,1}, J_{e,1}, \dots, J_{t,p}, J_{r,p}, J_{e,p}]^T$$

Result:

- Ordinary differential equation
- No constraint equations
- Combination of rigid + elastic bodies

## 3. Minimal coordinates

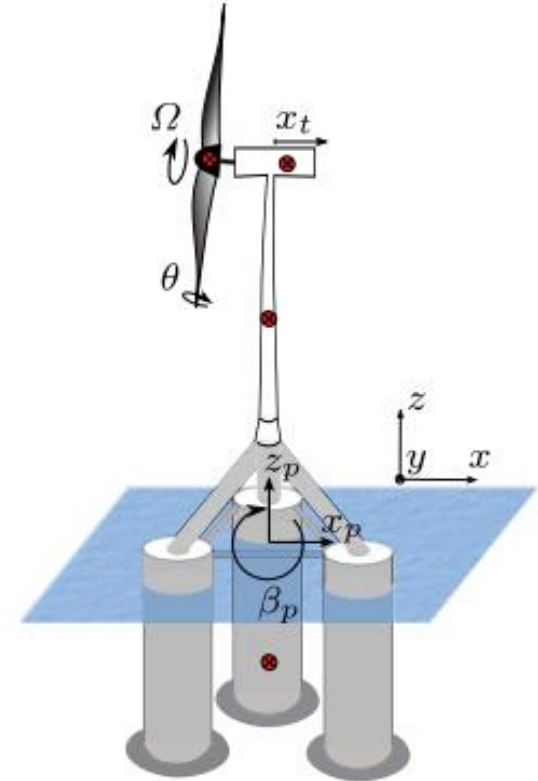
$$\bar{M}(q)\ddot{q} + \bar{h}_\omega(q, \dot{q}) = \bar{h}_g(q) + \bar{h}_d(q, \dot{q}) + \bar{h}_e(q_e)$$

$$q = [x_p, z_p, \beta_p, \varphi, x_t, \dots]^T$$

# Methodology: Newton-Euler Formalism

Pre-existing in-house model SLOW:

- Purpose:
  - Low-order model (~5-10 DOFs)
  - Quick design load assessment (3600x real time)
  - Nonlinear & linear state-space
- Symbolic programming
- Matlab-based

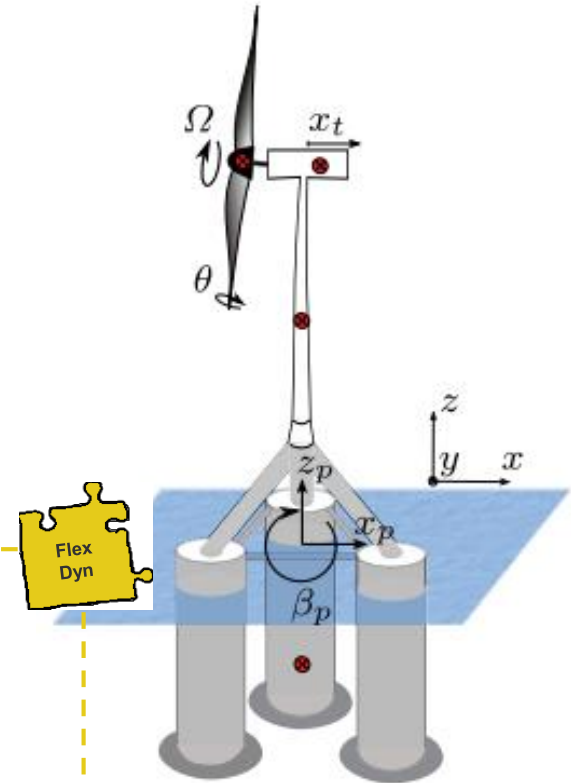
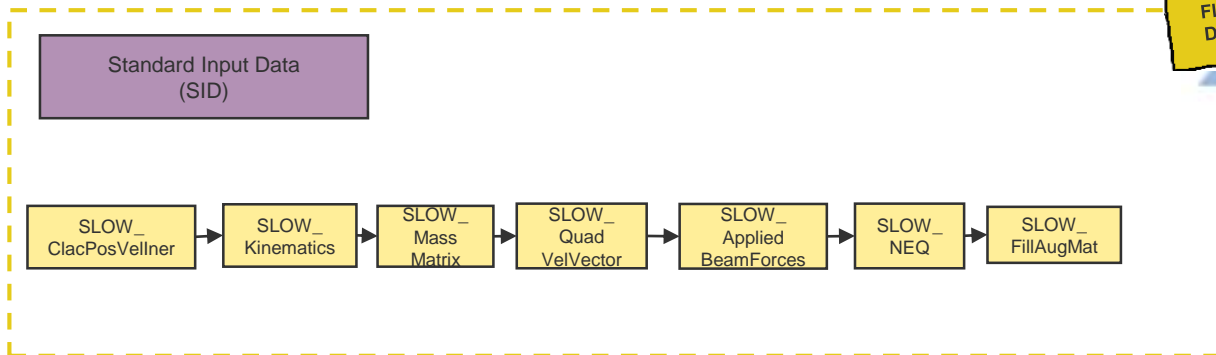




# Methodology: Newton-Euler Formalism

Pre-existing in-house model SLOW:

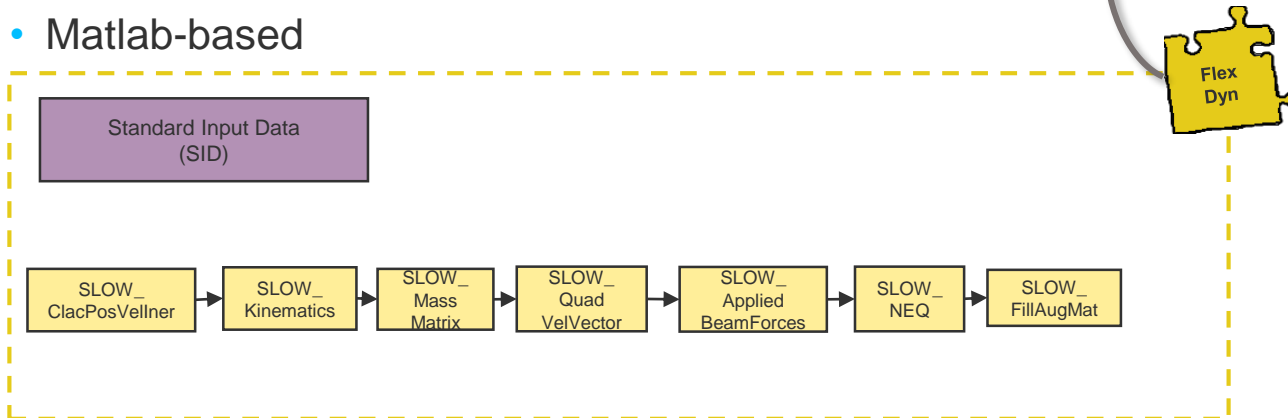
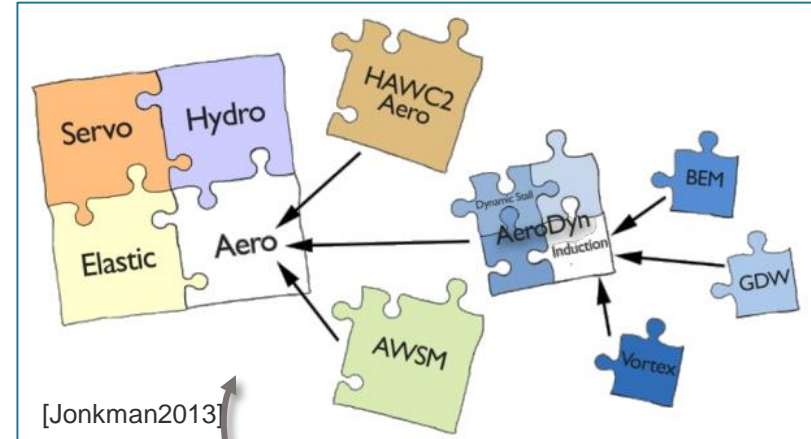
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Pre-existing in-house model SLOW:

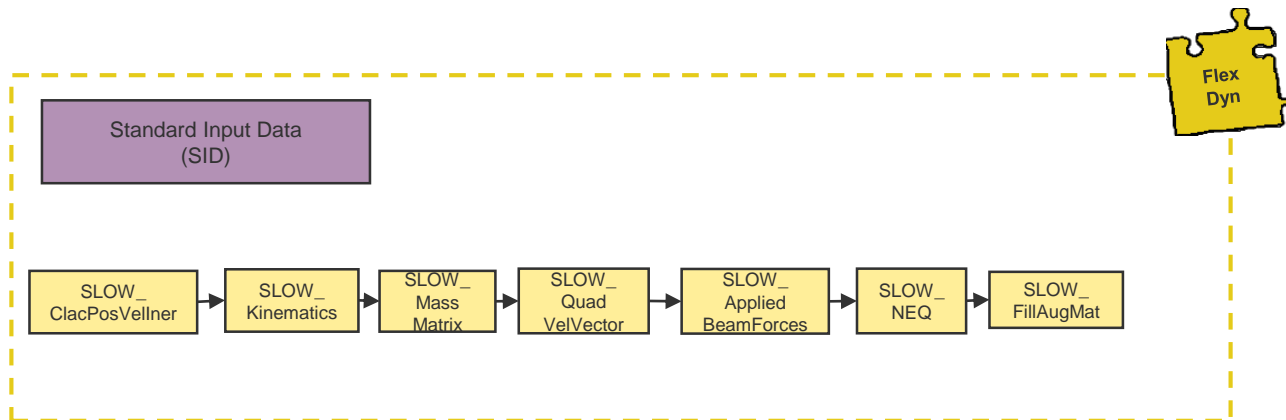
- Purpose:
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# Use-Case: Blades with Torsion-DOF

Steps:

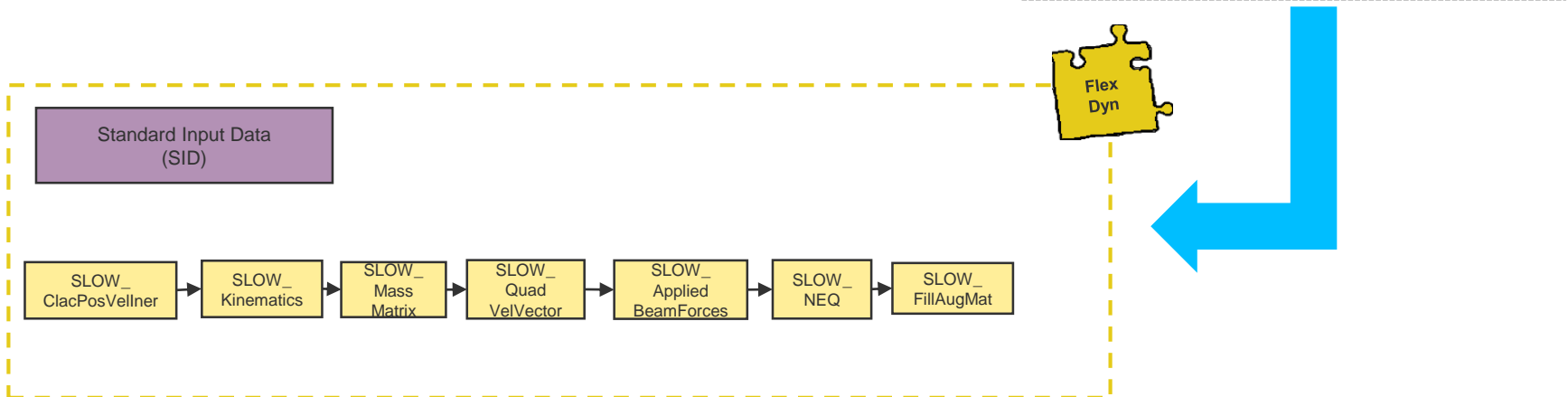
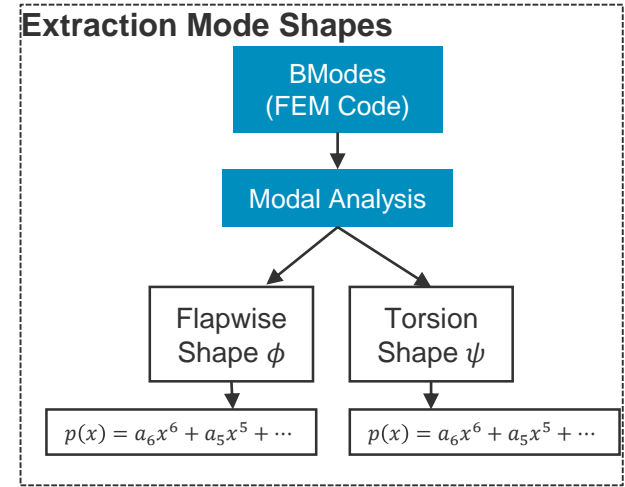
- User inputs:
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# Use-Case: Blades with Torsion-DOF

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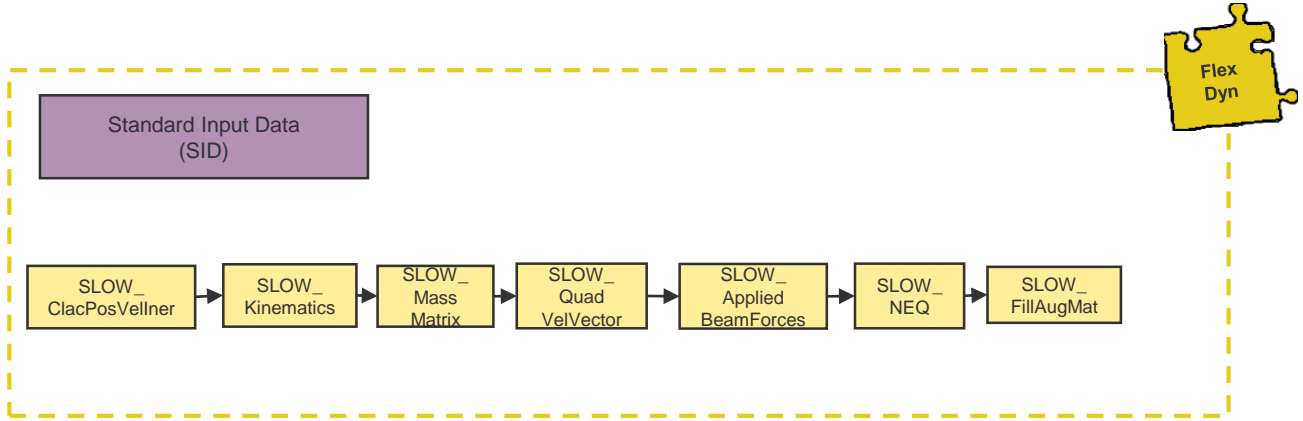
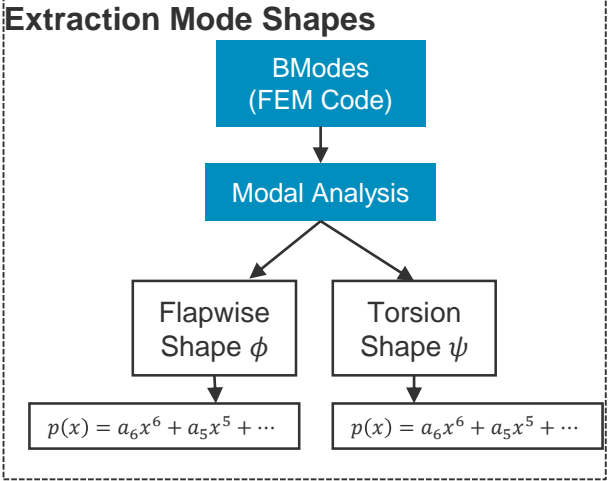
- User inputs:
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  - Distributed mass, elasticity
  - Shape functions



# Use-Case: Blades with Torsion-DOF

Verification: FEM vs. Modal reduction

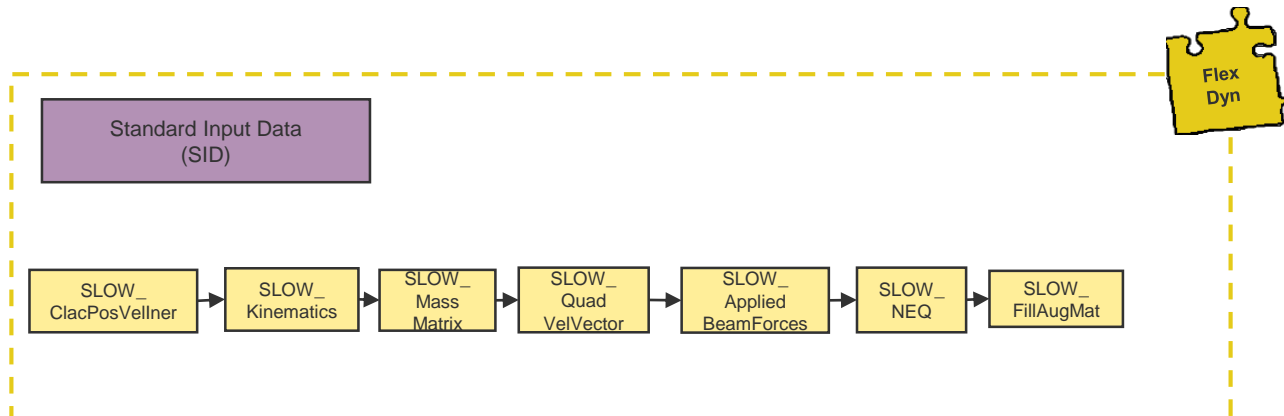
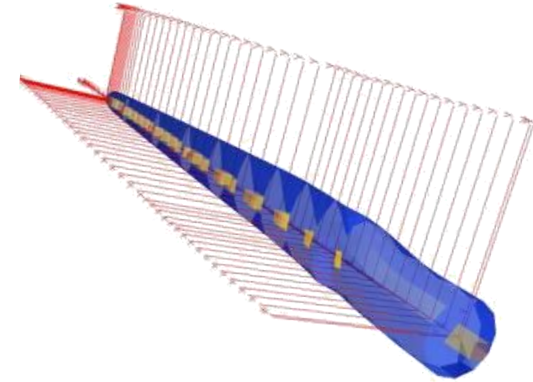
| Model     | Flapwise Frequency [ Hz ] | Error [%] |
|-----------|---------------------------|-----------|
| BModes    | 0.656                     | 0.0       |
| ElastoDyn | 0.629                     | 4.1       |
| FlexDyn   | 0.620                     | 5.5       |



# Use-Case: Blades with Torsion-DOF

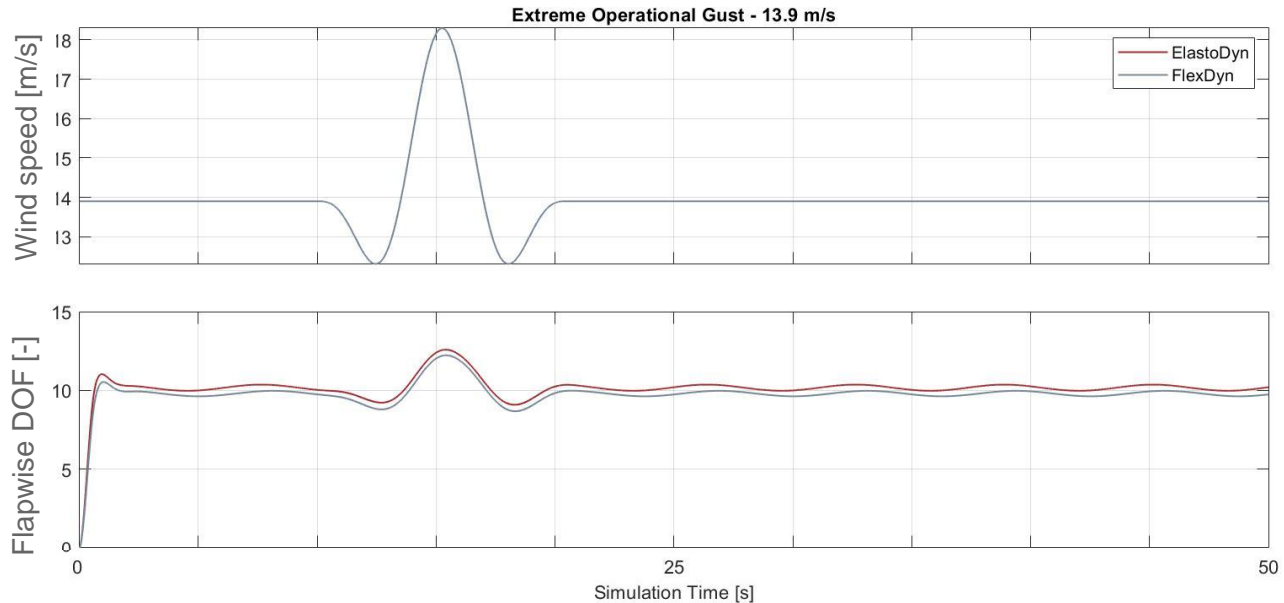
## Steps:

- User inputs:
  - Reference frame position, angular velocity
  - Distributed mass, elasticity
  - Shape functions
- AeroDyn: Generalized forces, kinematics



# Verification ElastoDyn vs. FlexDyn

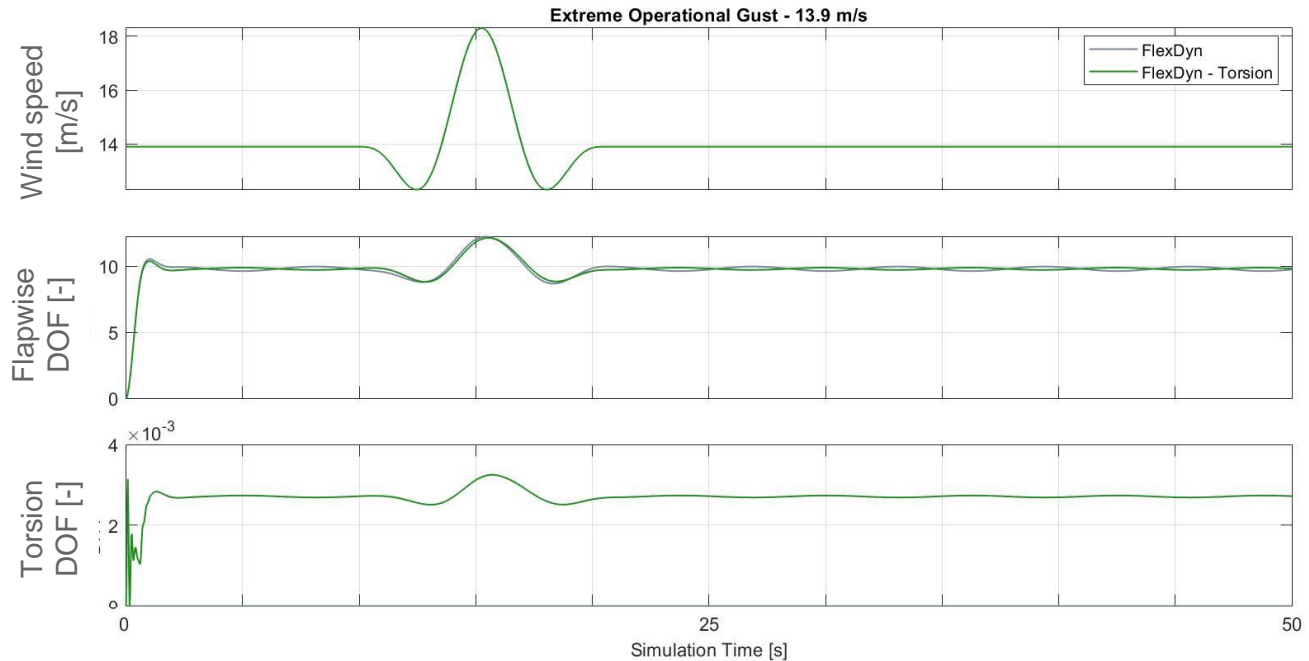
- Extreme Operating Gust:



➤ Good agreement of new FlexDyn with existing ElastoDyn

# Comparison Blade Torsion FlexDyn

- Extreme Operating Gust:



➤ Successful implementation of blade torsion.



# Summary & Conclusions

1. Newton-Euler formalism for Multibody Systems successfully implemented in OpenFAST framework
  2. First verifications show good agreement with existing ElastoDyn
  3. Added torsional degree of freedom with plausible results
- Next steps:
    - Verification
    - OpenFAST Modularization framework
    - Investigate potential to add FlexDyn into OpenFAST
    - Evaluate options for 3D shape functions
    - Incorporate Finite Element bodies into Multibody Equations





University of Stuttgart

Thank you!



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University of Stuttgart



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FKZ: 03EE2004A