

High-Entropy Hydrides for Fast and Reversible Hydrogen Storage at Room Temperature: Binding-Energy Engineering via First-Principles Calculations and Experiments

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Despite high interest in compact and safe storage of hydrogen in the solid-state hydride form, the design of alloys that can reversibly and quickly store hydrogen at room temperature under pressures close to atmospheric pressure is a long-lasting challenge. In this study, first-principles calculations are combined with experiments to develop high-entropy alloys (HEAs) for room-temperature hydrogen storage. $\text{Ti}_x\text{Zr}_{2-x}\text{CrMnFeNi}$ ($x = 0.4-1.6$) alloys with the Laves phase structure and low hydrogen binding energies of -0.1 to -0.15 eV are designed and synthesized. The HEAs reversibly store hydrogen in the form of Laves phase hydrides at room temperature, while (de)hydrogenation pressure systematically reduces with increasing the zirconium fraction in good agreement with the binding energy calculations. The kinetics of hydrogenation are fast, the hydrogenation occurs without any activation or catalytic treatment, and the storage capacity is higher than that for commercial LaNi_5 . The current findings demonstrate that a combination of theoretical calculations and experiments is a strong pathway to design new high-entropy hydrides with high performance for hydrogen storage.

Keywords: Solid-state hydrogen storage; Density functional theory (DFT); High-entropy alloy (HEA); Metal hydrides; Laves phase.

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1. Introduction

Excessive consumption of fossil fuels and CO₂ emission caused by their utilization have led to the crisis of global warming. Nowadays, finding clean fuels which do not emit CO₂ is a serious challenge for scientists and industry leaders. Hydrogen is the cleanest fuel and has attracted attention as a substitute for fossil fuels; however, besides the necessity for clean production of hydrogen, its safe and compact storage is a significant challenge [1]. Storage of hydrogen in the form of gas and liquid is conventionally used for various applications. However, the amount of stored hydrogen in the form of gas in typical commercial tanks with 225 liters and 20 MPa pressure is just 4 Kg [2]. Therefore, this typical method has limitations in terms of volumetric and gravimetric storage densities, although there are recent trends to increase the storage pressure to 70 MPa by using special tanks [1]. In the liquid storage method, the volumetric and gravimetric storage densities are higher, and the safety is better than for the gas storage method, but liquifying hydrogen at low temperatures makes the method expensive and evaporation losses can also occur [2]. Solid-state hydrogen storage particularly in the form of metal hydrides provides the most compact and safest technology to store hydrogen [2].

To realize the application of metal hydrides for hydrogen storage, they should have several features such as the capability for reversible absorption and desorption of hydrogen at ambient temperature, high cycling stability, fast kinetics, appropriate storage pressure near atmospheric pressure and high gravimetric capacity (high gravimetric capacity for stationary applications is not as critical as it is for mobile applications) [3]. Magnesium hydride and complex hydrides are well-known materials with high storage capacity, but they suffer from high thermodynamic stability, and thus, they function only at high temperatures [1]. So far, a limited number of materials such as TiFe (TiFeH₂) and LaNi₅ (LaNi₅H₆) have been introduced for room-temperature hydrogen storage [3-6], but they exhibit other shortcomings such as the activation problem in TiFe, and a high price and low storage capacity in LaNi₅ [3-6]. Therefore, there are still significant demands to introduce new metal hydride systems that can satisfy the requirements for hydrogen storage at ambient temperature.

High-entropy materials, which are solid solutions of at least five principal elements with a configurational entropy higher than $1.5R$ (R : gas constant), have attracted attention in recent years for various applications including hydrogen storage [7]. The presence of several elements in a single phase allows to manipulate the electronic structure, hydrogen binding energy and accordingly hydrogen storage temperature and pressure by careful selection of principal elements and their concentrations [7]. TiVZrNbHf [8-10], TiVCrNbMo [8], TiVCrNbTa [8], Ti_{0.2}Zr_{0.2}Hf_{0.2}Mo_{0.1}Nb_{0.3} [11], Ti_{0.2}Zr_{0.2}Hf_{0.2}Mo_{0.2}Nb_{0.2} [11], Ti_{0.2}Zr_{0.2}Hf_{0.2}Mo_{0.3}Nb_{0.1} [11], TiZrVNbCr [12], V₃₀Ti₃₀Cr₂₅Fe₁₀Nb₅ [13], V₃₅Ti₃₀Cr₂₅Fe₅Mn₅ [13], Mg_{0.10}Ti_{0.30}V_{0.25}Zr_{0.10}Nb_{0.25} [14], TiZrNbFeNi [15], TiZrNbCrFe [16], MgAlTiFeNi [17], Al_{0.10}Ti_{0.30}V_{0.25}Zr_{0.10}Nb_{0.25} [18], Mg₁₂Al₁₁Ti₃₃Mn₁₁Nb₃₃ [19], MgVAlCrNi [20], MgVTiCrFe [21], AlCrFeMnNiW [22], TiZrHfScMo [23], MgZrTiFe_{0.5}Co_{0.5}Ni_{0.5} [24] and LaNiFeVMn [25] are some of the HEAs which have been investigated for hydrogen storage. However, as discussed in a recent review paper [7], these HEAs have drawbacks such as either high temperature requirement for hydrogen storage, poor hydrogen storage reversibility, poor activation, or high storage pressure [8-25], which limit their applications. Although the research on high-entropy hydrogen storage materials is still at its early stages, designing these alloys by theoretical and computational methods is expected to provide a pathway to discover new materials that can quickly and reversibly store hydrogen at ambient conditions.

In this work, first-principles calculations are combined with experiments to design HEAs for room-temperature hydrogen storage. The designated alloys, Ti_xZr_{2-x}CrMnFeNi ($x = 0.4-1.6$) with the

Laves phase structure and low hydrogen binding energies of -0.1 to -0.15 eV, show fast and reversible hydrogen storage at ambient temperature under pressures adjustable to the atmospheric pressure by changing the amounts of titanium and zirconium. This simultaneous application of theoretical and experimental studies to high-entropy hydrogen storage materials confirms the significance of this strategy in developing new HEAs that can satisfy the requirements for stationary hydrogen storage applications.

2. Materials and methods

2.1. Empirical material design

The key issue in designing room-temperature hydrogen storage materials is to adjust the hydrogen binding energy to a negative value close to zero [26]. An earlier study on first-principles calculations of Mg-based alloys suggested that binding energies about -0.1 eV per hydrogen atom can be an appropriate target to achieve room temperature hydrogen storage [26]. Moreover, the hydrogen binding energy should be slightly more negative than -0.1 eV to reduce the equilibrium hydrogen storage pressure close to ambient pressure. Although such a concept has not been used to design HEAs so far, three empirical criteria were suggested by the current authors to achieve hydrogen storage at low temperatures in HEAs [27]: (i) AB₂-type atomic configuration (A: elements which react with hydrogen; B: elements with low affinity with hydrogen), (ii) C14 Laves phase structure formation in the alloy and hydride; and (iii) valence electron concentration (VEC) of 6.4.

- Hydrogen storage materials are usually a mixture of A-type elements (such as lanthanum, magnesium, titanium, etc.) and B-type elements (such as nickel, iron, manganese, etc.) [1]. The A-type elements have negative hydrogen binding energies and produce stable hydrides, while B-type elements have positive binding energies and usually do not absorb hydrogen, as schematically shown in Fig. 1a using the data reported in literature [3,26,28]. Therefore, a combination of A-type and B-type elements can lead to the formation of alloys with an appropriately low hydrogen binding energy for room-temperature hydrogen storage such as TiFe and LaNi₅ [1]. In this regard, it was found that AB₂-type HEAs have high potential for low-temperature hydrogen storage [27], while AB-type and A₃B₂-type systems are other candidates, yet with less potential [15,16].
- The Laves phase alloys are considered as potential materials for hydrogen storage with high cycling stability for reversible hydrogenation and dehydrogenation and fast kinetics [29]. Another benefit of Laves phase alloys is that they can have lower cost compared to rare-earth-based alloys such as LaNi₅ [29]. It was shown by both experiments and the CALPHAD (calculation of phase diagrams) method that the Laves phases can be formed in some high-entropy hydrogen storage systems such as Ti-Zr-Cr-Mn-Fe-Ni [27], Ti-Zr-Nb-Fe-Ni [15] and Ti-Zr-Nb-Cr-Fe [16].
- VEC is another key parameter which can be considered in designing alloys for reversible hydrogen storage at room temperature. Metals with low VEC such as lithium, magnesium and titanium usually produce stable hydrides, which can release hydrogen only at high temperatures, while metals with high VEC such as cobalt, nickel and copper usually exhibit low affinity with hydrogen. It was suggested that HEAs with a VEC values of 6.4 can desorb hydrogen at temperatures close to room temperature [8]. Although adjusting VEC is hard in simple binary or ternary alloys, it can be adjusted much easier in HEAs by changing the type and fraction of the principal elements.
- The hydrogen binding energy is the most important parameter that needs to be adjusted for reversible hydrogen storage at room temperature and under atmospheric pressures. The

dehydrogenation temperature increases and the equilibrium hydrogen pressure decreases with increasing the absolute value of negative binding energy. Only a limited number of materials such as LaNi_5 and TiFe show appropriate hydrogen binding energies for room-temperature hydrogen storage. As schematically shown in Fig. 1a, the target is to set the hydrogen binding energy to a value slightly more negative than -0.1 eV by adjusting the fraction of elements [26].

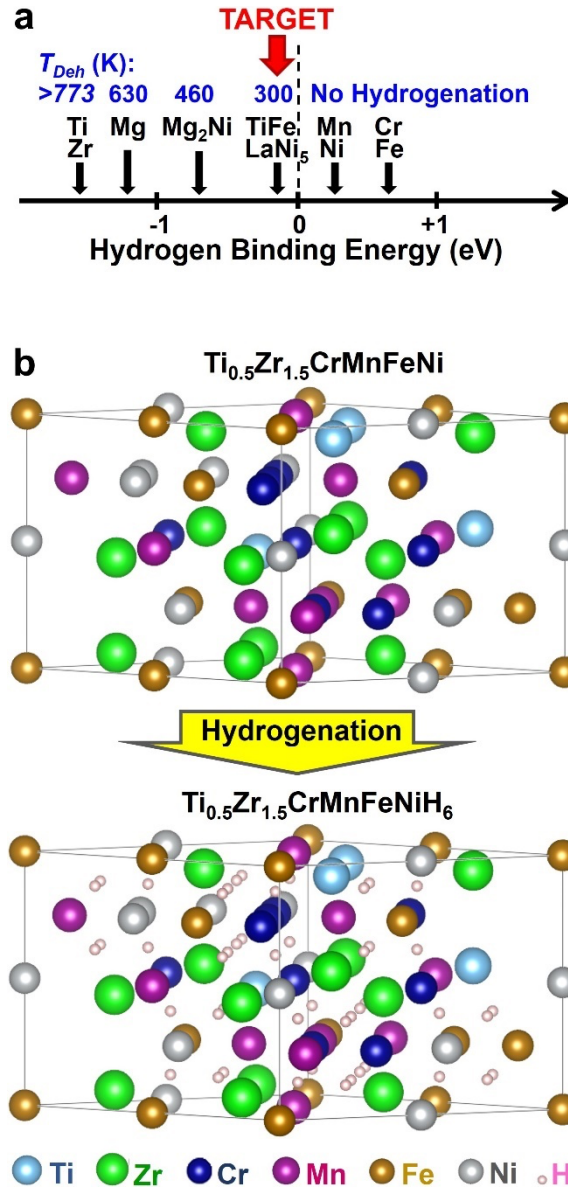


Fig. 1. (a) Schematic illustration of hydrogen binding energy on hydrogenation and dehydrogenation of different materials. Examples of structures of (b) HEA $\text{Ti}_{0.5}\text{Zr}_{1.5}\text{CrMnFeNi}$ and (c) high-entropy hydride $\text{Ti}_{0.5}\text{Zr}_{1.5}\text{CrMnFeNiH}_6$, modeled using SQS and visualized using VESTA.

Therefore, this study focuses on HEAs with the AB_2 -type Laves phase structure and a VEC value of 6.4; and among the available options, the Ti-Zr-Cr-Mn-Fe-Ni system can fit all these requirements [27]. The hydrogen binding energy is adjusted by changing the fraction of zirconium in balance with titanium, because zirconium has a higher atomic radius than the other elements in

this alloying system, and thus, adjusting its fraction is supposed to have the most significant effect on lattice volume and binding energy. Three compositions of $\text{Ti}_x\text{Zr}_{2-x}\text{CrMnFeNi}$ ($x = 0.5, 1.0, 1.5$) were theoretically studied by first-principles binding energy calculations and four compositions of $\text{Ti}_x\text{Zr}_{2-x}\text{CrMnFeNi}$ ($x = 0.4, 0.8, 1.2, 1.6$) were experimentally examined by hydrogen storage characterizations.

2.2. First-principles calculation methods

2.2.1. Crystal structure modeling of alloys

The AB_2 -type hexagonal C14 Laves phases have the space group of $P6_3/mmc$ (No.194), in which the A-type atoms occupy the $4f$ Wyckoff sites, and the B-type atoms occupy the $2a$ and the $6h$ Wyckoff sites [29,30]. These phases have in total 12 atoms in their unit cell. If A and B atoms in the AB_2 -type Laves phases are approximated by close-packed rigid spheres with the radii r_A and r_B , respectively, the ratio r_A/r_B is given by $\sqrt{3}/2 \approx 1.225$ [30]. These atomic positions in the close-packing case, which are considered as the ideal positions, lead to a c/a ratio of $\sqrt{8}/3 \approx 1.633$ (a and c are lattice parameters).

The C14 $\text{Ti}_x\text{Zr}_{2-x}\text{CrMnFeNi}$ Laves phase alloys ($x = 0.5, 1.0, 1.5$) were modeled using 48-atom supercells with a $2 \times 2 \times 1$ expansion of the primitive cell of the C14 phase. The A sites were occupied by titanium and zirconium, and the B sites were occupied by chromium, manganese, iron, and nickel. The sublattice chemical disorder was modeled using special quasi-random structure (SQS) configurations [31]. Correlation functions of the first several nearest-neighbor doublet, triplet, and quartet clusters were optimized to be close to the ideal values of fully random configurations using the simulated annealing approach implemented in the ICET code [32]. To achieve better statistics, six different configurations were considered for each composition by permuting the elements.

2.2.2. Crystal structure modeling of hydrides

To model the structure of the high-entropy hydrides, crystallographic information and reports from literature were considered. There are few calculation reports on high-entropy Laves phase hydrides, but it is experimentally known that the HEAs which have the Laves phase also produce hydrides with the Laves phase [15,16,27]. Moreover, it was reported that the Laves phase alloys with an AB_2 -type composition produce Laves phase hydrides with an AB_2H_3 -type composition [27]. In the Laves phase alloys, there are 17 tetrahedral interstitial sites per formula unit AB_2 , which could be occupied by hydrogen atoms. These interstitial sites are surrounded by either four B atoms (B_4), one A and three B atoms (AB_3), or two A and two B atoms (A_2B_2). For many conventional Laves phases composed of elements similar to those in the present study, previous *ab initio* simulations found that the A_2B_2 sites are the most energetically preferable sites for hydrogen atoms [33-38], and indeed many experiments found hydrogen atoms at the A_2B_2 sites [39-47]. This may be intuitively understood because the A_2B_2 sites have larger volumes than the B_4 and AB_3 sites when the atoms A and B are on the ideal Laves lattice sites, as summarized in Table 1. The hydrogen atoms in Laves phases should also be repulsive to each other and should not occupy very close interstitial sites, as empirically suggested [48] and confirmed by first-principles calculations for some Laves phases [35,38].

Therefore, to model the Laves phase hydrides with a composition of $\text{Ti}_x\text{Zr}_{2-x}\text{CrMnFeNiH}_6$, it was assumed that the hydrogen atoms occupy some A_2B_2 sites that are distant from each other. To satisfy this condition, all hydrogen atoms were put at the $12k$ A_2B_2 tetrahedral sites, which do not share the faces of the tetrahedra with each other [49]. Fig. 1 shows examples of modeled structures

of (b) an alloy and (c) its corresponding hydride which were modeled using SQS [31] and visualized using VESTA [33].

Table 1. Numbers of tetrahedral interstitial sites per formula unit AB_2 and their volumes with respect to formula unit volume in Laves phases with ideal atomic positions.

Tetrahedra Site	Number	Volume
B_4	1	1/24 (~0.0417)
AB_3	4	5/96 (~0.0521)
A_2B_2	12	1/16 (= 0.0625)

2.2.3. Hydrogen binding energy calculations

Ab initio density functional theory (DFT) calculations were performed using the VASP code [50-52] with the plane-wave basis projector augmented wave (PAW) method [53]. The exchange-correlation energy was obtained within the generalized gradient approximation (GGA) of the Perdew-Burke-Ernzerhof (PBE) form [54]. The plane-wave cutoff energy was set to 400 eV. Reciprocal spaces were sampled by a Γ -centered $4 \times 4 \times 6$ k -point mesh for the 48-metal-atom supercell models and the Methfessel-Paxton method [55] with the smearing width of 0.1 eV. The 3d 4s orbitals of titanium, chromium, manganese, iron, and nickel and the 4s 4p 4d 5s orbitals of zirconium were treated as the valence states. Total energies were minimized until they converged within 1×10^{-3} eV per simulation cell for each ionic step. All calculations were performed by considering spin polarization, a fact that was also confirmed experimentally by magnetic measurements, as discussed in Appendix and Fig. A1.

To obtain the energy-volume curves, seven volumes in the ranges of 144 to 180 $\text{\AA}^3/\text{u.c.}$ and 186 to 222 $\text{\AA}^3/\text{u.c.}$ (u.c.: unit cell) were considered for the systems with and without hydrogen atoms, respectively. For each composition, the obtained energies of six SQS-based models for the given volumes were then fitted to the Vinet equation of state [56,57] to obtain the volume and the energy in the equilibrium state. Metal and hydrogen atoms were initially put on the ideal Laves-phase lattice sites and the geometric centers (centroids) of the A_2B_2 $12k$ interstitial sites, respectively. The atomic positions were then relaxed with fixing the cell shape and volume until all the forces on the atoms converged within 5×10^{-2} eV/ \AA . The hydrogen binding energy per atom was then computed as

$$\Delta E_H = \frac{1}{3} \left[E(AB_2H_3) - E(AB_2) - \frac{3}{2} E(H_2) \right] \quad (1)$$

where $E(H_2)$, $E(AB_2)$, and $E(AB_2H_3)$ are the energies of H_2 , AB_2 , and AB_2H_3 per formula unit, respectively. The energy of the H_2 molecule was computed in a $20 \times 20 \times 20 \text{\AA}^3$ simulation cell and for the Γ point in the reciprocal space. The obtained hydrogen-hydrogen distance was 0.751 \AA , in reasonable agreement with the experimental value of 0.74144 \AA [58].

2.3. Experimental Procedures

The ingots of HEAs $Ti_xZr_{2-x}CrMnFeNi$ ($x = 0.4, 0.6, 1.2$ and 1.6) with ~ 10 g mass were prepared by arc melting using pieces of pure titanium (99.99%), zirconium (99.5%), chromium (99.99%), manganese (99.95%), iron (99.97%) and nickel (99.9%). The pieces were melted and mixed in a water-cooled copper crucible under an argon atmosphere. To increase the homogeneity

of the alloys, the mixture was remelted six times. Ingots produced by arc melting were characterized by various methods, as described below.

First, the crystal structure was examined by X-ray diffraction (XRD) using Cu K α irradiation with a filament current of 40 mA and an acceleration voltage of 45 kV. The Rietveld method using the PDXL software was used to identify the phases and determine their lattice parameters.

Second, the microstructure of the samples was investigated by a scanning electron microscope (SEM) equipped with energy-dispersive X-ray spectroscopy (EDS) and electron backscatter diffraction (EBSD) at 15 kV. The samples for SEM were prepared by cutting a piece of the ingot using electric discharge machining, followed by mechanical grinding using sandpapers, polishing using buff and 9 μm and 3 μm diamond suspensions, and final polishing by buff and colloidal silica with 60 nm particle size.

Third, the nanostructure of the samples was examined using transmission electron microscopy (TEM) and scanning-transmission electron microscopy (STEM) at 200 kV using high-resolution imaging, fast Fourier transform (FFT) analysis and EDS analysis. For TEM and STEM analyses, a small piece of the samples was crushed in ethanol and dispersed on a carbon grid.

Fourth, hydrogen storage was examined using a Sieverts-type gas absorption apparatus at room temperature (298 K). For this experiment, ~ 1 g of the alloys was crushed in air atmosphere to achieve particle sizes below 100 μm . The crushed samples were examined in terms of pressure-composition-temperature (PCT) isotherms for three hydriding-dehydriding cycles followed by a hydrogenation kinetic measurement for one cycle. The samples before PCT measurements were subjected to evacuation at room temperature for 3 h to remove air and moisture, but no thermal activation treatment was performed. The crystal structure of the hydrides after hydrogen storage was also examined by conducting the XRD analysis immediately after hydriding.

3. Results

3.1. Calculated hydrogen binding energy

Figs. 2a, c and e show the *ab initio* computed energy-volume curves before and after relaxation of atomic positions for the $\text{Ti}_x\text{Zr}_{2-x}\text{CrMnFeNi}$ alloys with $x = 0.5, 1.0$ and 1.5 , respectively. For all compositions, the equilibrium unit cell volume decreases with increasing the fraction of titanium. Moreover, the equilibrium unit cell volume decreases after the relaxation, as summarized in Table 2. Fig. 2b, d and f show the *ab initio* computed energy-volume curves before and after relaxation of atomic positions for the $\text{Ti}_x\text{Zr}_{2-x}\text{CrMnFeNiH}_6$ hydrides with $x = 0.5, 1.0$ and 1.5 , respectively. In these hydrides, hydrogen atoms occupy all the $12k$ A_2B_2 interstitial sites. The unit cell volume of the hydride increases with increasing the titanium fraction. This trend is similar to the trend for the HEAs, but as summarized in Table 2, a main difference is that the unit cell volumes for the hydrides are 21-23% larger compared to the corresponding alloys (i.e., larger by 3 \AA^3 per hydrogen atom). Such a volume expansion is in a similar order to those experimentally reported for various binary and ternary hydrides [59] and also similar to the one previously calculated by *ab initio* for the $\text{Zr}(\text{Cr}_{0.5}\text{Ni}_{0.5})_2$ alloy with the C14 Laves phase (3.2 \AA^3 per hydrogen atom) [37]. Another difference between the alloys and hydrides is that the impact of atomic-position relaxation on the equilibrium volume and energy changes is much larger for the hydrides compared to the alloys, implying that the positions of metal atoms more strongly deviate from the ideal lattice sites due to the presence of hydrogen atoms.

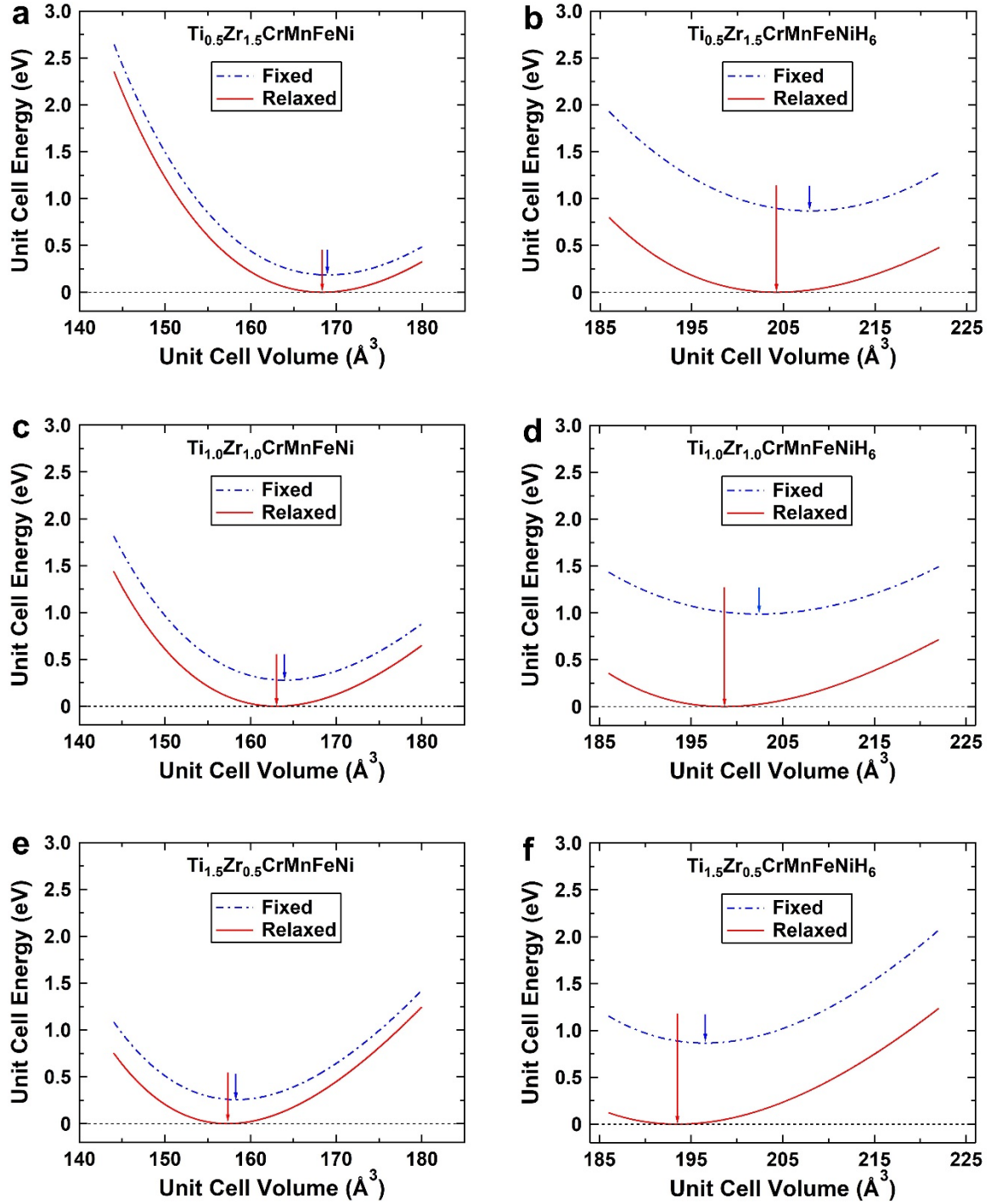


Fig. 2. *Ab initio* calculated energy-volume curves fitted to the Vinet equation of state without (fixed) and with relaxation of atomic positions for (a, c, e) HEAs $Ti_xZr_{2-x}CrMnFeNi$ and (b, d, f) corresponding high-entropy hydrides. Arrows show equilibrium volumes for fixed the relaxed atomic positions.

The hydrogen binding energy per H atom for relaxed atomic positions is given in [Table 2](#) for the three high-entropy hydrides $Ti_xZr_{2-x}CrMnFeNiH_6$. The hydrogen binding energies are -0.126, -0.105 and -0.074 eV per hydrogen atom for $x = 0.5, 1.0$ and 1.5 , respectively. These values are substantially lower than those at the A_2B_2 sites in the Laves phases consisting of similar elements but

chemically less disordered such as -0.27 eV per hydrogen atom for TiCr₂ [35], and -0.20 to -0.28 eV per hydrogen atom for Zr(Cr_{0.5}Ni_{0.5})₂ [37]. This implies that the present Laves HEAs can more easily desorb the hydrogen atoms, and thus, can be more practical for applications where low-temperature hydrogen storage is needed. Fig. 3 visualizes the dependence of the H binding energy as a function of the titanium content for relaxed atomic positions. With increasing the titanium content, the hydrogen binding energy becomes less negative, and thus the hydrides become less stable. Therefore, it is expected that the alloys with lower titanium content can desorb hydrogen at lower temperatures and lower pressures. The hydrogen binding energies for Ti_{0.5}Zr_{1.5}CrMnFeNiH₆ and Ti_{1.0}Zr_{1.0}CrMnFeNiH₆ are slightly more negative than -0.1 eV, suggesting the potential of these two alloys for room-temperature hydrogen storage [29]. The strong dependence of the hydrogen binding energy on the composition also indicates the possibility to tailor the properties of hydrogen storage alloys by modifying the compositions of HEAs [60].

Table 2. *Ab initio* calculated equilibrium volumes for fixed and relaxed atomic positions, unit cell energy difference between fixed and relaxed conditions, and hydrogen binding energy for HEAs Ti_xZr_{2-x}CrMnFeNi and their corresponding Ti_xZr_{2-x}CrMnFeNiH₆ hydrides where hydrogen atoms occupy all the 12k A₂B₂ interstitial sites.

Alloy/Hydride	Volume (Å ³ /u.c.)		$E_{\text{Relaxed}} - E_{\text{Fixed}}$ (Å ³ /u.c.)	ΔE_{H} (eV / H atom)
	Fixed	Relaxed		
Ti _{0.5} Zr _{1.5} CrMnFeNi	169.0	168.3	-0.18	
Ti _{1.0} Zr _{1.0} CrMnFeNi	164.0	163.0	-0.28	
Ti _{1.5} Zr _{0.5} CrMnFeNi	158.3	157.3	-0.26	
Ti _{0.5} Zr _{1.5} CrMnFeNiH ₆	207.8	204.2	-0.87	-0.126
Ti _{1.0} Zr _{1.0} CrMnFeNiH ₆	202.4	198.6	-0.99	-0.105
Ti _{1.5} Zr _{0.5} CrMnFeNiH ₆	196.5	193.5	-0.87	-0.074

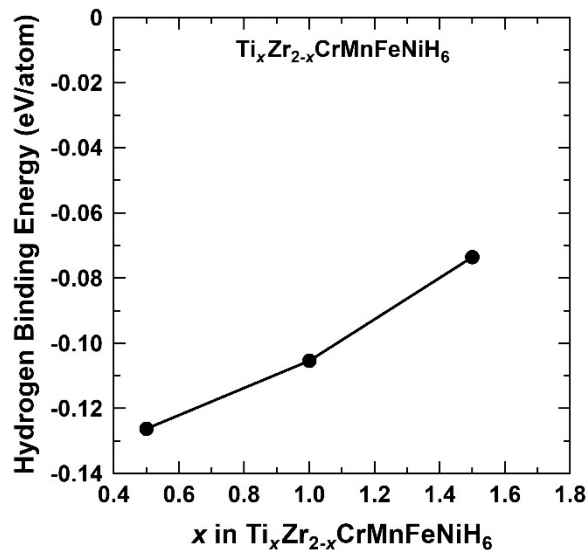


Fig. 3. *Ab initio* calculated hydrogen binding energy as a function of titanium content for high-entropy hydrides Ti_xZr_{2-x}CrMnFeNiH₆. Atomic positions were relaxed for these calculations.

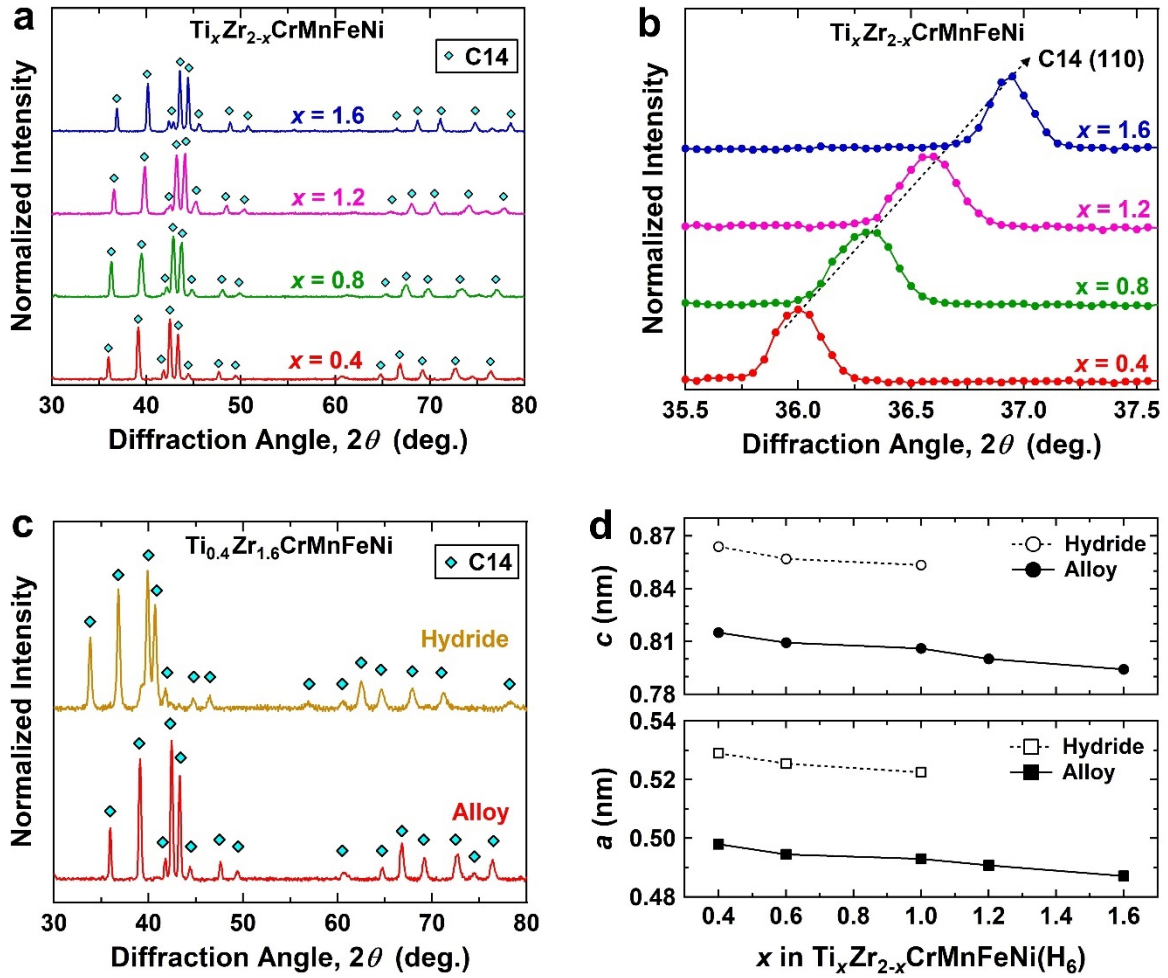


Fig. 4. (a, b) XRD profiles of HEAs $\text{Ti}_x\text{Zr}_{2-x}\text{CrMnFeNi}$ where (b) shows magnified view of (110) peak of C14 Laves phase, (c) XRD profiles of HEA $\text{Ti}_{0.4}\text{Zr}_{1.6}\text{CrMnFeNi}$ and corresponding high-entropy hydride, and (d) lattice parameters of HEAs $\text{Ti}_x\text{Zr}_{2-x}\text{CrMnFeNi}$ and corresponding high-entropy hydrides determined from XRD profiles using Rietveld method. Data for $\text{Ti}_{1.0}\text{Zr}_{1.0}\text{CrMnFeNi}$ in (d) were taken from literature [27].

3.2. Structural features of alloys and hydrides

Fig. 4 summarizes the results of the XRD analysis. **Fig. 4a** shows the XRD profiles of the HEAs, $\text{Ti}_x\text{Zr}_{2-x}\text{CrMnFeNi}$ ($x = 0.4-1.6$). All samples have mainly a hexagonal C14 Laves phase structure with the $P6_3/mmc$ space group, while the presence of weak peaks at $42-43^\circ$ for the Ti-rich alloys suggests that minor amounts of a cubic phase can also be present [27]. **Fig. 4b** shows a magnified view of the XRD profiles for the (110) peak of the Laves phase located between 35.5° and 37.5° . This figure demonstrates a systematic shift of this peak to higher angles with increasing titanium fraction, indicating that a lattice contraction occurs by increasing the titanium fraction. **Fig. 4c** compares the XRD pattern of $\text{Ti}_{0.4}\text{Zr}_{1.6}\text{CrMnFeNi}$ before and after hydriding. The hydride phase also has a hexagonal C14 crystal structure, while the shift of the XRD profile to lower angles after hydriding suggests that the lattice is expanded in the presence of hydrogen atoms in the lattice. **Fig. 4d** summarizes the lattice parameters calculated from the XRD analysis for both alloys and hydrides. It should be noted that the data for $\text{Ti}_{1.0}\text{Zr}_{1.0}\text{CrMnFeNi}$ was calculated from the XRD profiles reported in an earlier publication [27]. It should be also noted that the crystal structure of the

$\text{Ti}_{1.2}\text{Zr}_{0.8}\text{CrMnFeNiH}_6$ and $\text{Ti}_{1.6}\text{Zr}_{0.4}\text{CrMnFeNiH}_6$ hydrides could not be identified because these two hydrides released hydrogen very fast under ambient conditions and before the XRD analysis. Both a and c lattice parameters increase with increasing the amount of zirconium atoms which have a large atomic radius [61]. Moreover, the lattice parameters increase with the addition of hydrogen atoms to the materials.

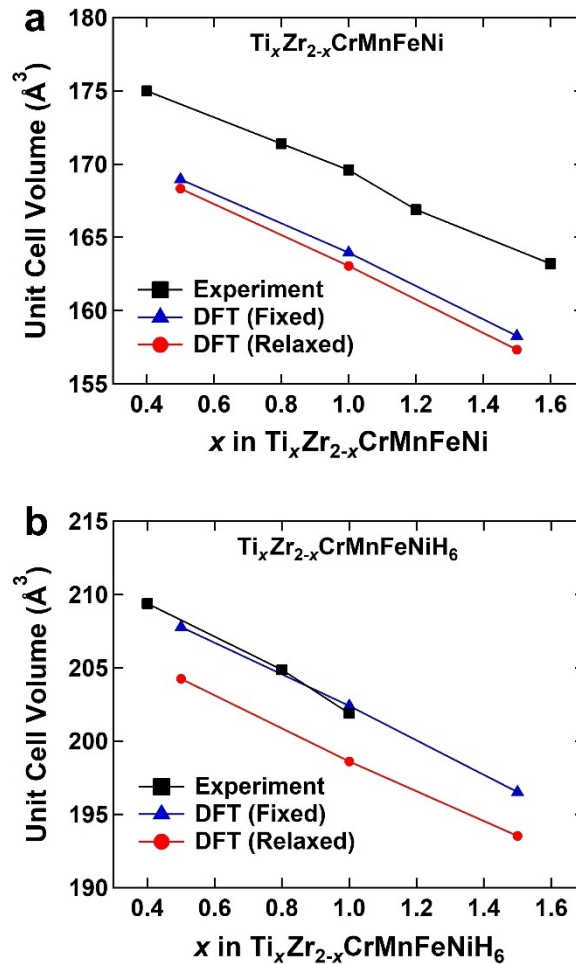


Fig. 5. Unit cell volume of C14 Laves phase obtained experimentally using XRD analysis and calculated using *ab initio* without (fixed) and with relaxation of atomic positions for (a) HEAs $\text{Ti}_x\text{Zr}_{2-x}\text{CrMnFeNi}$ and (b) corresponding high-entropy hydrides.

It is now possible to compare the unit cell volumes obtained experimentally and theoretically to validate the models used for the first-principles calculations. Fig. 5 compares the equilibrium volumes obtained by DFT with those obtained experimentally for the (a) alloys and (b) hydrides with different fractions of titanium. The experimental and theoretical data show similar trend, and the unit cell volume decreases with increasing the titanium content for both alloys and hydrides. The linear change in the unit cell volume is qualitatively consistent with Vegard's law by considering the difference in the atomic radius of titanium and zirconium [61]. The *ab initio* calculated volumes are slightly smaller than those obtained in experiments: 3.5% for the alloys and 2.5% for the hydrides. Such an underestimation of volume using GGA (such as PW91 [62,63] or PBE [54]) is found often

in systems containing magnetic 3d elements such as pure bcc iron [64-66] and the HEA CrMnFeCoNi [67,68]. The small differences between the experimental and theoretical cell volumes confirm the validity of the models used for the simulation of the HEAs and hydrides.

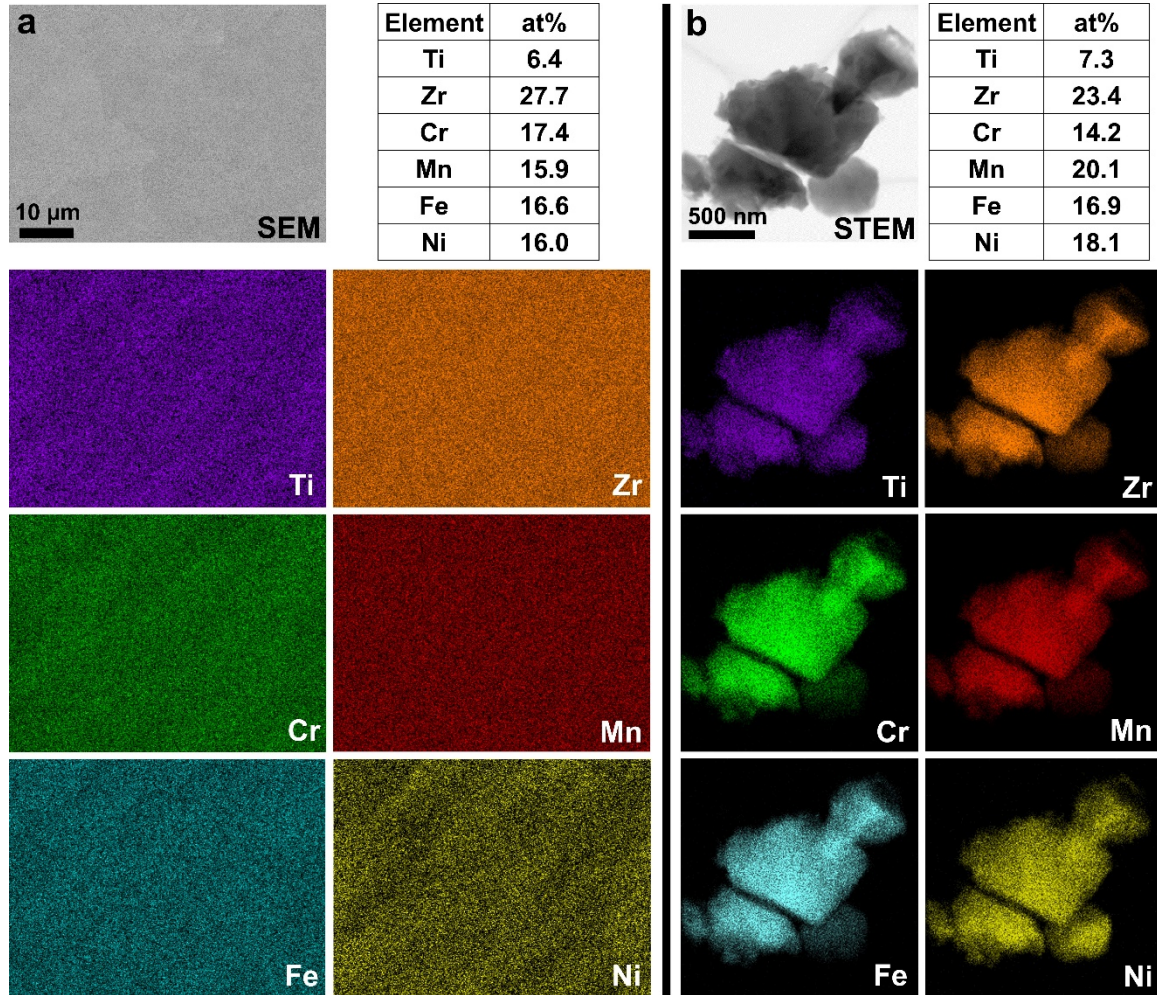


Fig. 6. Distribution of elements and their atomic fractions in HEA $Ti_{0.4}Zr_{1.6}CrMnFeNi$ examined by EDS elemental mappings using (a) SEM and (b) STEM.

3.3. Microstructure of alloys

The microstructure of $Ti_{0.4}Zr_{1.6}CrMnFeNi$, taken as a representative alloy with the lowest hydrogen binding energy, is shown in Figs. 6 and 7. Fig. 6 shows (a) SEM-EDS and (b) STEM-EDS analyses. The distribution of elements is reasonably uniform at the micrometer and nanometer levels. Moreover, the fraction of elements is reasonably consistent with the nominal composition within the detection limits of EDS analysis. The EDS analysis confirms that the arc melting can be successfully employed to synthesize the HEAs. An SEM micrograph and corresponding EBSD crystal orientation and phase mappings are shown in Figs. 7a-c, respectively. Fig. 7b illustrates that the HEA includes mainly large and elongated grains with sizes of several hundred micrometers and Fig. 7c confirms that the alloy contains mainly a C14 Laves phase in good agreement with the XRD analysis. Figs. 7d-f show the high-resolution TEM images of the HEA. The C14 Laves phase was the only phase

that could be detected by high-resolution TEM images in good agreement with the XRD and EBSD analyses. Most of the examined regions such as the one in Fig. 7d are free from defects, while high-angle grain boundaries and dislocations are visible in some regions, as shown in Figs. 7e and 7f, respectively. These microstructural features are rather similar to the microstructures of other Laves phases synthesized by arc melting [15,16,27].

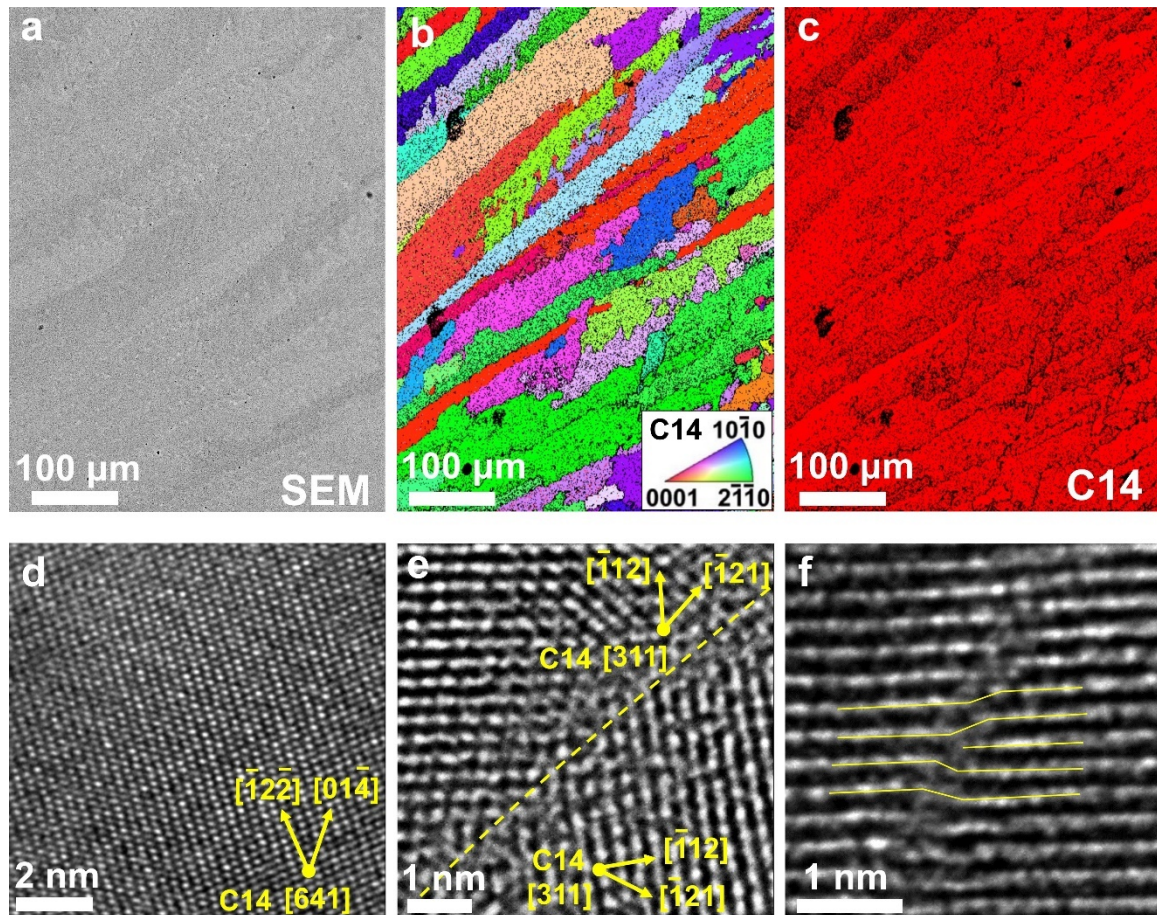


Fig. 7. (a) SEM micrograph and corresponding (b) crystal orientation and (c) phase mappings achieved by EBSD with beam step size of 1 μm ; and (d-f) high-resolution TEM lattice images for (d) C14 Laves phase lattice, (e) high-angle grain boundary and (f) dislocation for HEA $\text{Ti}_{0.4}\text{Zr}_{1.6}\text{CrMnFeNi}$.

3.4. Room temperature hydrogen storage

Figs. 8a-d show the PCT absorption/desorption isotherms for three cycles at 298 K for the $\text{Ti}_x\text{Zr}_{2-x}\text{CrMnFeNi}$ alloys with $x = 0.4, 0.8, 1.2$ and 1.6 , respectively. Fig. 8a indicates that the $\text{Ti}_{0.4}\text{Zr}_{1.6}\text{CrMnFeNi}$ alloy reversibly absorbs and desorbs 1.7 wt% of hydrogen with good cycling performance. The maximum hydrogen-to-metal (H/M) ratio for the alloy reaches 1.06, confirming that the composition of the hydride can be reasonably considered as $\text{Ti}_{0.4}\text{Zr}_{1.6}\text{CrMnFeNiH}_6$. PCT isotherms for the $\text{Ti}_{0.8}\text{Zr}_{1.2}\text{CrMnFeNi}$ alloy in Fig. 8b shows a similar trend as for $\text{Ti}_{0.4}\text{Zr}_{1.6}\text{CrMnFeNi}$. Further, the alloy can store 1.6 wt% of hydrogen with a hydrogen-to-metal ratio of 1, corresponding to the $\text{Ti}_{0.8}\text{Zr}_{1.2}\text{CrMnFeNiH}_6$ hydride. A main difference between Figs. 8a and

8b is that the alloy with lower Ti exhibits a lower plateau pressure which should be due to its stronger hydrogen binding energy, as discussed with respect to Fig. 3. Fig. 8c shows the PCT isotherms for the $\text{Ti}_{1.2}\text{Zr}_{0.8}\text{CrMnFeNi}$ sample. This HEA absorbs 1.4 wt% hydrogen with a hydrogen-to-metal ratio of 0.8. Since the plateau pressure for this alloy is high, its complete hydrogenation does not occur by increasing the pressure to 9 MPa (i.e., upper limit of pressure in the authors' gas absorption facility). As shown in Fig. 8d, the $\text{Ti}_{1.6}\text{Zr}_{0.4}\text{CrMnFeNi}$ alloy absorbs a minor amount of 0.1 wt% hydrogen, suggesting that the plateau pressure of this alloy is higher than 9 MPa because of its weak hydrogen binding energy, as discussed in Fig. 3.

Fig. 8e provides a clear comparison between the PCT isotherms in the third absorption cycle for the $\text{Ti}_x\text{Zr}_{2-x}\text{CrMnFeNi}$ alloys with $x = 0.4, 0.8, 1.0, 1.2$ and 1.6 , where the data for the $\text{Ti}_{1.0}\text{Zr}_{1.0}\text{CrMnFeNi}$ alloy were taken from literature [27]. The plateau pressure systematically increases by increasing the fraction of titanium, while the $\text{Ti}_{0.4}\text{Zr}_{1.6}\text{CrMnFeNi}$ and $\text{Ti}_{0.8}\text{Zr}_{1.2}\text{CrMnFeNi}$ alloys have plateau pressures close to ambient pressure which renders them appropriate for practical applications. Such an increase in the plateau pressure by increasing the Ti content can be well explained by the influence of titanium on the hydrogen binding energy, as shown in Fig. 3.

Fig. 9 demonstrates the kinetic measurements of hydrogen storage under an initial hydrogen pressure of 3.7 MPa at room temperature for the HEAs. The alloys absorb hydrogen very fast within almost 30 seconds, although the total amount of hydrogen decreases with increasing the fraction of titanium, i.e., with increasing the plateau pressure. The amount of stored hydrogen in $\text{Ti}_{0.4}\text{Zr}_{1.6}\text{CrMnFeNi}$ in both kinetic and PCT measurements is higher than the capacity of commercial room-temperature hydrogen storage materials [1-6].

4. Discussion

HEAs are the most recent alloys which have been explored for hydrogen storage [8-25]. The presence of multi-principal elements in the lattice of these alloys makes it possible to tune their electronic structures, crystal structures and physical properties in a much more straightforward way as compared to conventional alloys and intermetallics [7]. Since the capability to store hydrogen strongly depends on the electronic structure [1-3], the flexibility in controlling the electronic structure of HEAs introduces them as potential materials for hydrogen storage applications. However, the investigations on high-entropy hydrogen storage materials are still in their infancy, and only a few attempts have been pursued to combine theoretical calculations and experiments to develop new HEAs with appropriate electronic structures for room-temperature hydrogen storage [7]. The current study addresses this challenge and combines the existing empirical knowledge on the development of HEAs for low-temperature hydrogen storage with first-principles calculations to design alloys that can reversibly store hydrogen at ambient temperature under pressures close to atmospheric pressure. The empirical knowledge suggests that HEAs with AB_2 -type Laves phase structure and a VEC close to 6.4 have a high potential for low-temperature hydrogen storage [8,15,16,27]. Previous first-principles calculations on conventional Mg-based alloys also suggest that a hydrogen binding energy of -0.1 eV or slightly more negative can lead to room-temperature hydrogen storage [26]. The $\text{Ti}_x\text{Zr}_{1-x}\text{CrMnFeNi}$ alloys were therefore selected for the present study because they satisfy all empirical requirements and their theoretical hydrogen binding energy can be tuned to negative values smaller than -0.1 eV by changing the fraction of titanium and zirconium atoms.

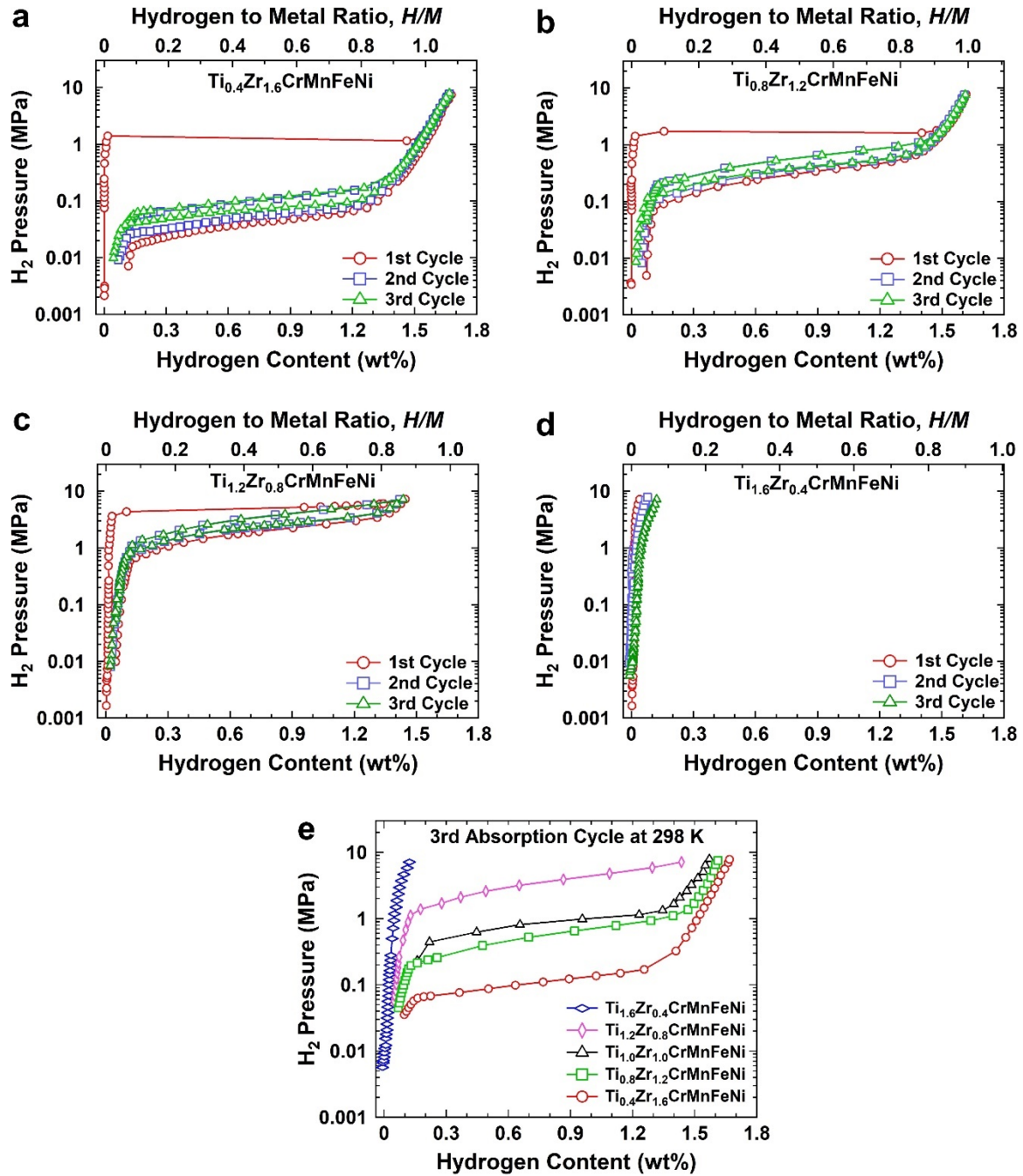


Fig. 8. PCT absorption/desorption isotherms at room temperature for HEAs (a) $\text{Ti}_{0.4}\text{Zr}_{1.6}\text{CrMnFeNi}$, (b) $\text{Ti}_{0.8}\text{Zr}_{1.2}\text{CrMnFeNi}$, (c) $\text{Ti}_{1.2}\text{Zr}_{0.8}\text{CrMnFeNi}$ and (d) $\text{Ti}_{1.6}\text{Zr}_{0.4}\text{CrMnFeNi}$; and (e) comparison of third cycle of PCT absorption isotherms for HEAs. Data for $\text{Ti}_{1.0}\text{Zr}_{1.0}\text{CrMnFeNi}$ in (e) were taken from literature [27].

The designed alloys reversibly adsorb and desorb hydrogen at room temperature, while the equilibrium pressure can be easily tuned to appropriately low values by reducing the hydrogen binding energy to more negative values via increasing the fraction of zirconium. The kinetics of hydrogen storage is quite fast in these alloys due to their Laves phase structure [29]. Moreover, such fast storage kinetics occur without any thermal activation or catalyst addition, in contrast to many other storage materials including TiFe which suffer from the activation problem at room temperature

[3,5]. Another advantage is that the good hydrogen storage performance of the present HEAs was achieved even though they were handled and crushed under an air atmosphere. Such a good air resistance cannot be achieved easily for other room-temperature hydrogen storage materials without conducting chemical modification [3] or mechanical treatment through severe plastic deformation [69]. Among the selected alloys in this study, the amount of stored hydrogen in $\text{Ti}_{0.4}\text{Zr}_{1.6}\text{CrMnFeNi}$ and $\text{Ti}_{0.8}\text{Zr}_{1.2}\text{CrMnFeNi}$ alloys is higher than the capacity of commercial rare-earth-based LaNi_5 for room-temperature hydrogen storage [4,70,71]. The working pressure of these two alloys is also close to atmospheric pressure, in good agreement with their hydrogen binding energies, suggesting their high potential for stationary applications [1,2]. Therefore, a combination of first-principles calculations and experimental studies is an effective approach to design and synthesize new high-entropy hydrides for room-temperature hydrogen storage. Such an approach can also contribute to the advancement of nickel-metal-hydride (Ni-MH) batteries because HEAs were recently reported to have high potential as anode materials of Ni-MH batteries [72].

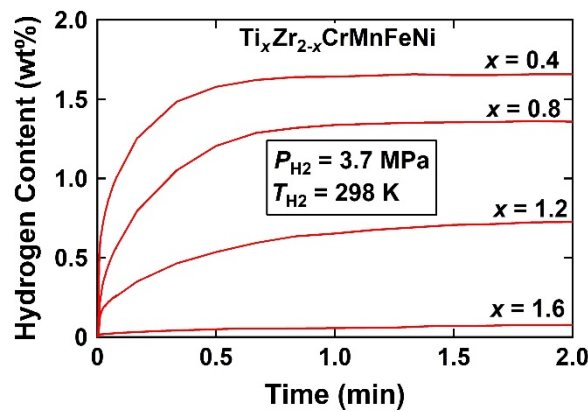


Fig. 9. Hydrogenation kinetic curves at room temperature for HEAs $\text{Ti}_x\text{Zr}_{2-x}\text{CrMnFeNi}$.

5. Conclusion

This study demonstrates the successful design and synthesis of high-entropy alloys having the capability to store hydrogen at room temperature and under pressures close to atmospheric pressures. The AB_2 -type Laves phase $\text{Ti}_x\text{Zr}_{2-x}\text{CrMnFeNi}$ ($x = 0.4-1.6$) alloys with a valence electron concentration of 6.4 and low hydrogen binding energies (negative values close to -0.1 eV) were designed theoretically by using first-principles calculations and fabricated experimentally by the conventional arc melting method. These alloys reversibly absorb and desorb up to 1.7 wt% of hydrogen at room temperature (298 K) with fast kinetics, while their (de)hydrogenation pressure is systematically reduced by strengthening the hydrogen binding energy through increasing the zirconium fraction. To the authors' knowledge, this study is the first demonstration of adjusting the hydrogen storage temperature and pressure of high-entropy alloys to ambient conditions by employing the concept of binding-energy engineering. The concept introduced in the current study can be universally employed to discover a large number of hydrogen storage materials for practical applications.

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Appendix

Magnetic properties of a Ti-rich alloy and a Ti-poor alloy were examined at 5 K and 300 K using a superconducting quantum interference device (SQUID) magnetometer. Fig. A1 shows the variations of magnetization versus magnetic field for (a) $\text{Ti}_{0.4}\text{Zr}_{1.6}\text{CrMnFeNi}$ and (b) $\text{Ti}_{1.6}\text{Zr}_{0.4}\text{CrMnFeNi}$. Both alloys are paramagnetic at cryogenic and ambient temperatures and do not show a clear ferromagnetic behavior. These magnetic tests confirm that the assumption of non-magnetism used for first-principles calculations is reasonable.

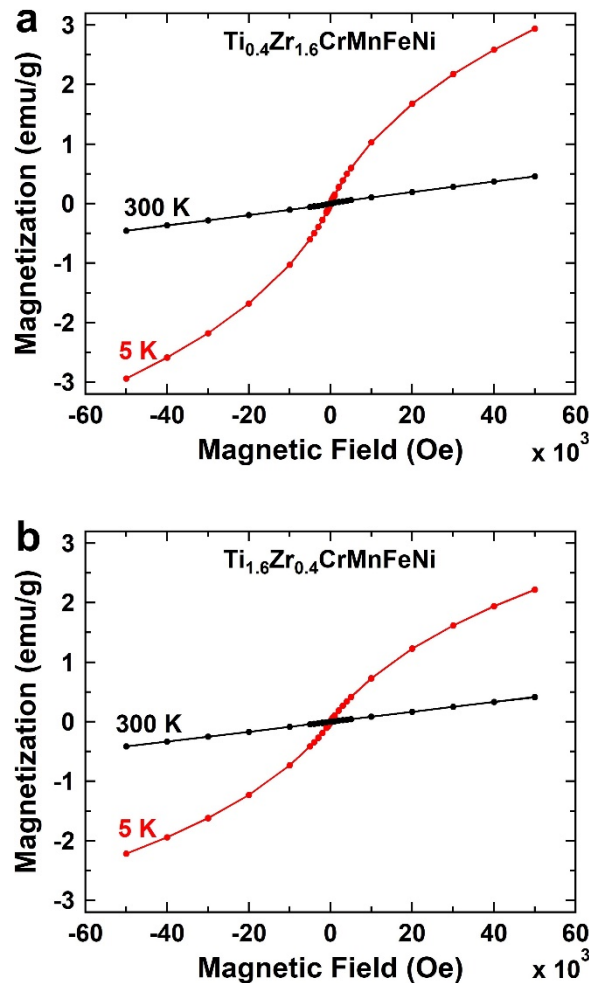


Fig. A1. Magnetization versus magnetic field examined using SQUID at 5 K and 300 K for HEAs (a) $\text{Ti}_{0.4}\text{Zr}_{1.6}\text{CrMnFeNi}$ and (b) $\text{Ti}_{1.6}\text{Zr}_{0.4}\text{CrMnFeNi}$.

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