

## Electrons and holes in InSb under crossed magnetic and stress fields. III. Magnetoreflexion

B. Wolfstädter\*

*Physikalisches Institut, Universität Würzburg, D-8700 Würzburg, West Germany*

H.-R. Trebin

*Institut für Theoretische und Angewandte Physik, Universität Stuttgart,  
D-7000 Stuttgart 80, West Germany*

H. Pascher

*Physikalisches Institut, Universität Bayreuth, D-8580 Bayreuth, West Germany*

H. G. Häfele

*Physikalisches Institut, Universität Würzburg, D-8700 Würzburg, West Germany*

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We have investigated the electronic interband transitions close to the band gap of InSb by observing magnetoreflexivity under uniaxial stress. The sensitivity of the experiment was increased by application of a magnetic-field-modulation technique. By this method we can resolve transitions from the conduction band to various valence-band Landau levels. The measurements were carried out with light polarized linearly along and perpendicular to the magnetic induction  $\mathbf{B}$  ( $E_{\parallel}\mathbf{B}$  and  $E_{\perp}\mathbf{B}$ ). In addition to well-known electric dipole resonances we observed new transitions induced by stress. These additional lines are connected with transition matrix elements which arise from lowering the symmetry. The observed transition energies are compared with band-structure calculations.

### I. INTRODUCTION

The optical reflectivity of a semiconductor is, in general, modified by uniaxial stress.<sup>1</sup> The changes depend on the direction of stress, the Landau-level structure of the material, and the wavelength and polarization of light. They are most pronounced near the onset of the direct interband transitions and thus yield information about the levels involved. In InSb the valence-band Landau levels are anomalously spaced due to the degeneracy of heavy and light holes at  $\mathbf{k}=0$ .<sup>2</sup> By applying stress  $T_{\parallel}[100]$  and magnetic field  $\mathbf{B}_{\parallel}[001]$  the symmetry of InSb is lowered to  $C_2$ . In paper II of the current series of articles, this fact proved helpful in identifying optical transitions.<sup>3</sup> There, we explored interband transitions by optically pumped stimulated recombination radiation and measured the stress dependence of the valence-band levels  $2V$  and  $3V$  which carry oscillator and angular momentum quantum numbers  $(0, \frac{1}{2})$  and  $(0, -\frac{1}{2})$ , respectively. Due to the different carrier occupation, in absorption other transitions are observed than in luminescence. But radiation with energy exceeding the fundamental gap is only transmitted by very thin samples which cannot be exposed to uniaxial stress. Therefore we decided to observe direct interband magneto-optical transitions using the reflection technique.<sup>4</sup>

### II. EXPERIMENTAL TECHNIQUE

Reflection measurements are performed with photon energies, which differ only slightly from the gap energy of

InSb. As a light source we used a liquid-nitrogen-cooled cw CO laser. A grating in the resonator made the laser emit one single vibration-rotation line. The sample was mounted in the Voigt configuration in the center of a split-coil superconducting magnet and was immersed in superfluid helium of 1.5 K.

The reflected radiation was detected with a cooled (77 K) Ge: Au detector. Because of the large dielectric constant the reflectivity of InSb is also very high (about 0.36) and is barely influenced by electronic interband transitions. To detect small changes caused by magneto-optical interband resonances it was necessary to apply a magnetic-field-modulation technique.<sup>5,6</sup> For this purpose an additional normal-conducting coil was fixed in the cryostat of the superconducting magnet, so that a sinus-shaped alternating field could be superposed to the static magnetic field. A modulation amplitude of  $7 \times 10^{-3}$  T proved suitable for our experiments. Only that part of the reflected radiation is measured which is produced by the periodic modulation of the magnetic field. It is separated by a lock-in amplifier, whose output is proportional to the first derivative of the reflectivity with respect to the magnetic field. Using constant laser frequencies this first derivative is recorded as a function of the magnetic field. By integration of the traces we recover the reflectivity.

Samples were cut from single crystals of  $p$ -doped InSb with carrier concentrations  $p \leq 10^{14} \text{ cm}^{-3}$ . We used either cleaved surfaces or etched them by CP4.<sup>7</sup> It was found that the signal amplitudes strongly depend on the preparation of the sample surface.

III. EXPERIMENTAL RESULTS  
IN UNSTRESSED MATERIAL

For perpendicular incidence of the light the reflection coefficient is calculated as

$$R = \frac{(n - 1)^2 + \kappa^2}{(n + 1)^2 + \kappa^2},$$

where  $n$  is the real part and  $\kappa$  the imaginary part of the complex refractive index.  $\kappa$  changes resonantly in a magnetic field if the photon energy of the incident radiation coincides with the level spacing of an interband transition. Near the band gap there is a large dispersion.  $R$  as a function of  $B$  displays a dispersive line shape if the transition energy of an allowed interband transition is tuned through the fixed photon energy.<sup>8</sup> The resonant magnetic field can be taken from the point of inflection of this curve. In the measured first derivative this point shows up as a peak. Two typical recorder traces of  $dR/dB$  as a function of the magnetic field at constant laser frequency are presented in Fig. 1. In Fig. 1(a) the electric field vector  $\vec{E}$  of the linearly polarized laser beam is parallel, in Fig. 1(b) perpendicular to the magnetic field  $\vec{B}$ . Three sharp resonances corresponding to interband transitions appear in each trace. The shift caused by many-body interactions<sup>9</sup> between free carriers can be neglected, since we used  $p$  material with very small carrier densities and low sample temperatures. By means of the modulation technique we could resolve several transitions from valence-band levels near the edge to the  $n=0$  and  $n=1$  Landau levels of the conduction band with spin up or spin down, respectively. An identification of the different valence-band levels was possible by making use of the selection rules and the polarization characteristics.

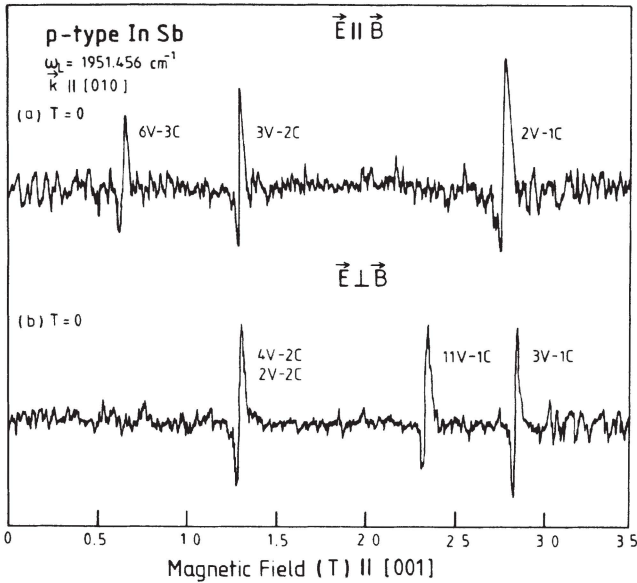


FIG. 1. Magnetoreflexion of  $p$ -type InSb for (a)  $\vec{E} \parallel \vec{B}$  and (b)  $\vec{E} \perp \vec{B}$  interband transitions. Laser frequency  $1951.456 \text{ cm}^{-1}$ ,  $\vec{B} \parallel [001]$ ,  $\vec{k} \parallel [010]$ , stress  $T = 0$ .

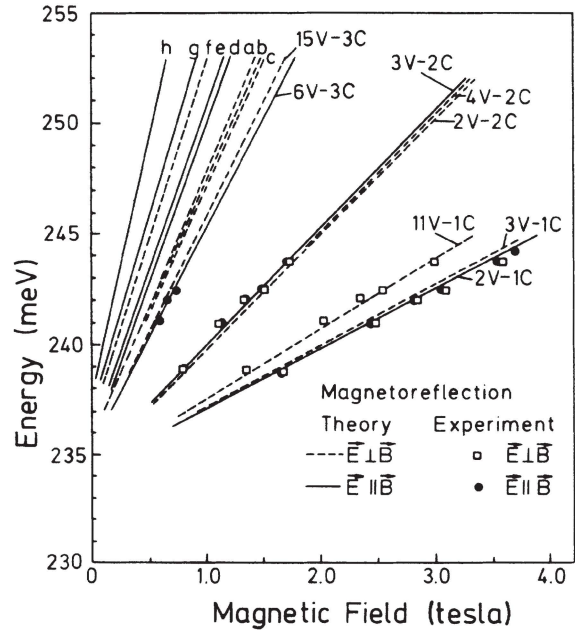


FIG. 2. Comparison of the theoretical energies of interband transitions with the resonances determined by magnetoreflexion in unstrained material. The lines were calculated with a band parameter set  $\gamma_1 = 37.1$ ,  $\gamma_2 = 16.5$ ,  $\gamma_3 = 17.7$ , and  $\kappa = 15.6$ , the remaining parameters being taken as in Ref. 10. All the lines have been shifted by 1 meV to lower energies. The theoretical lines at high energies are related with the following transitions: (a)  $1V \rightarrow 1C$ , (b)  $7V \rightarrow 3C$ , (c)  $6V \rightarrow 4C$ , (d)  $7V \rightarrow 4C$ , (e)  $12V \rightarrow 1C$ , (f)  $10V \rightarrow 5C$ , (g)  $2V \rightarrow 6C$ , and (h)  $1V \rightarrow 5C$ .

The results for the unstrained material, plotted in terms of photon energy versus magnetic field, are shown in Fig. 2 and are compared to theoretical calculations. There is an interband transition in  $\vec{E} \parallel \vec{B}$  polarization connecting the heavy-hole level  $6V$  with the conduction-band level  $3C$  (for the labeling of the levels see Ref. 10). Further transitions lead from  $3V$ ,  $2V$ , and  $4V$  to the  $2C$  conduction-band level. The  $2V \rightarrow 2C$  and  $4V \rightarrow 2C$  transitions are polarized  $\vec{E} \perp \vec{B}$  and have nearly the same energy, so that their lines cannot be resolved. The oscillator strength of  $4V \rightarrow 2C$  is almost twice that of  $2V \rightarrow 2C$ , therefore this transition contributes most to the resonance. The transition  $3V \rightarrow 2C$  is excited only in polarization  $\vec{E} \parallel \vec{B}$ . Within the measuring accuracy the resonant magnetic field cannot be distinguished from that of the transitions  $2V \rightarrow 2C$  and  $4V \rightarrow 2C$ .

For the final state  $1C$  three transitions are observed:  $11V \rightarrow 1C$ ,  $3V \rightarrow 1C$ , and  $2V \rightarrow 1C$ . Without stress, the transition  $4V \rightarrow 1C$ , which should have almost the same energy as  $2V \rightarrow 1C$ , is forbidden. The transitions  $11V \rightarrow 1C$  and  $3V \rightarrow 1C$  appear in polarization  $\vec{E} \perp \vec{B}$ , while  $2V \rightarrow 1C$ , starting from a heavy-hole level, is excited in polarization  $\vec{E} \parallel \vec{B}$ . The resonances belonging to  $2V \rightarrow 1C$  and  $3V \rightarrow 1C$  are separated distinctly in our experimental spectra. Compared to the theoretical prediction, the transition  $3V \rightarrow 1C$  displays a smaller energy, in agreement with the experimental results described in paper II.<sup>3</sup>



#### IV. INTERBAND TRANSITIONS UNDER UNIAXIAL DEFORMATION

Figure 3 shows experimental traces for several stress values recorded with frequency  $\omega_L = 1943.535 \text{ cm}^{-1}$  and polarization  $\vec{E} \perp \vec{B}$ . In the uppermost curve (stress  $T=0$ ) we can recognize the same structures as discussed in Sec. III. The transition  $3V \rightarrow 1C$  occurs with the highest oscillator strength. Applying uniaxial stress of 38 MPa to the sample only two resonances persist. The transition  $11V \rightarrow 1C$  disappears, while  $3V \rightarrow 1C$  is shifted to lower magnetic fields. With increasing stress the resonant magnetic field for  $3V \rightarrow 1C$  is further reduced, whereas the  $2V \rightarrow 2C$  structure tends slightly towards higher fields. These experimental features are well explained by the stress dependence of the energy levels calculated in paper I [Fig. 2(b)]. When increasing stress from zero value the

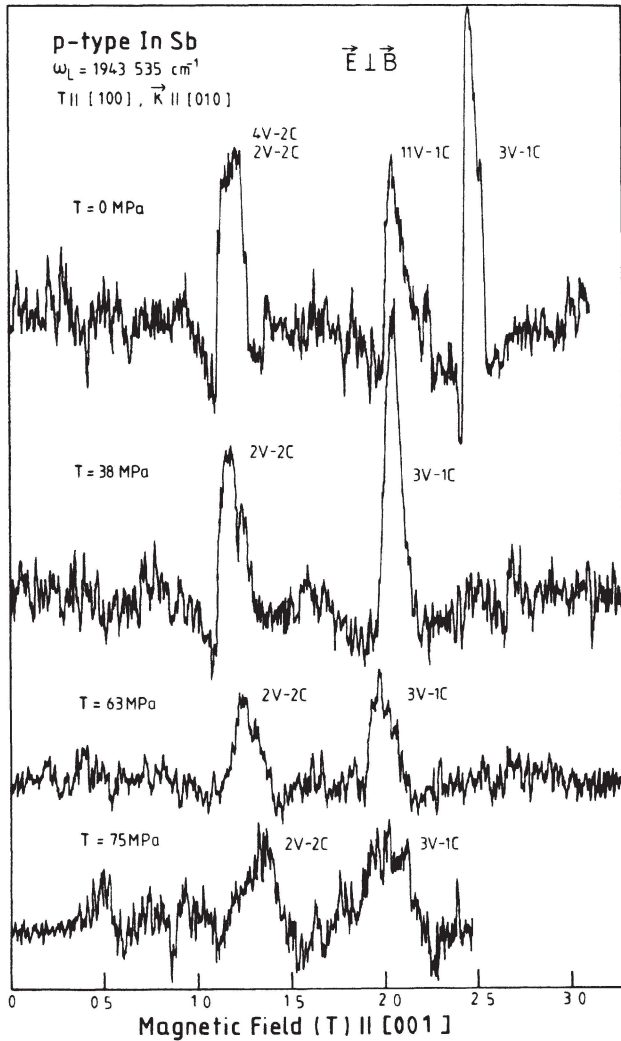


FIG. 3. Magnetoreflexion under different uniaxial deformations.  $\vec{B} \parallel [001]$ , laser frequency  $1943.535 \text{ cm}^{-1}$ , polarization perpendicular to the magnetic field.

energy of the  $3V$  level rises until about 100 MPa is reached. Therefore, the transition  $3V \rightarrow 1C$  always takes place at lower magnetic fields. The same argument holds for  $11V \rightarrow 1C$ , but the oscillator strength is strongly diminished and the structure can no longer be observed at 38 MPa. Since the energy of the  $2V$  level decreases with increasing stress, higher magnetic fields are necessary for the  $2V \rightarrow 2C$  resonance at higher stress. In Fig. 4 the magnetoreflexion is shown for the same laser line as in Fig. 3, but with polarization  $\vec{E} \parallel \vec{B}$ . The resonance of the transition  $2V \rightarrow 1C$  shifts to higher magnetic fields with increasing stress. This behavior again corresponds to the calculated energy diagram, where the energy difference is diminished with increasing deformation. The valence-band levels  $2V$  and  $3V$  are of special interest at low stress down to  $T=0$ , because below 30 MPa transitions involving the  $2V$  level could not be observed in stimulated recombination radiation (paper II). Under uniaxial deformations greater than 30 MPa the emission frequencies show a linear behavior for the  $2V$  level. Our magnetoreflexion measurements indicate that for  $T < 30$  MPa the  $2V$  energy remains nearly constant.

For polarization  $\vec{E} \parallel \vec{B}$  at 38 MPa two new structures appear, which are associated with higher Landau levels in the valence band. The increasing oscillator strength of

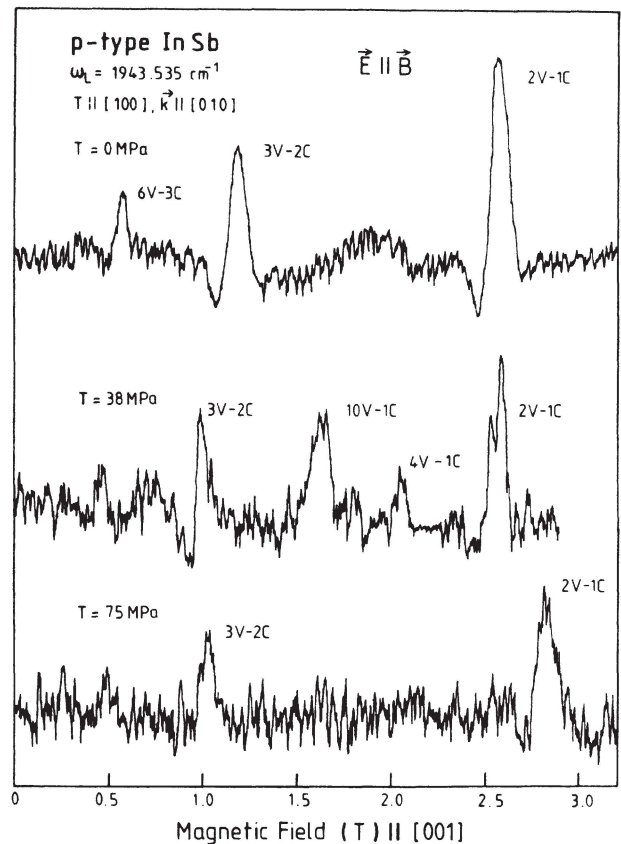


FIG. 4. Magnetoreflexion under different uniaxial stresses.  $\vec{B} \parallel [001]$ , laser frequency  $1943.535 \text{ cm}^{-1}$ , polarization  $\vec{E} \parallel \vec{B}$ .

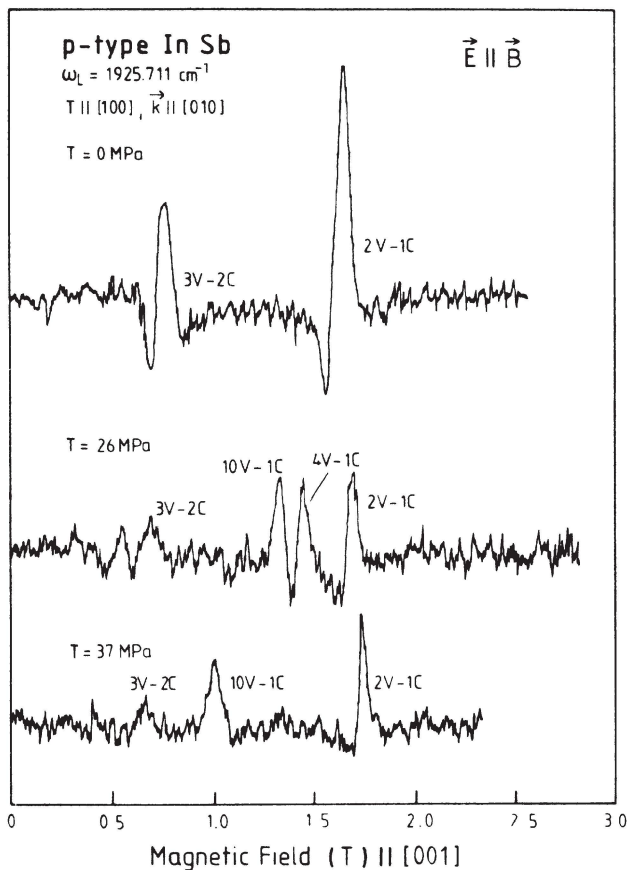


FIG. 5. Magnetoreflection under different uniaxial deformations.  $\mathbf{B} \parallel [001]$ , laser frequency  $1925.711 \text{ cm}^{-1}$ , polarization  $\mathbf{E} \parallel \mathbf{B}$ .

the transitions  $10V \rightarrow 1C$  and  $4V \rightarrow 1C$  at small stresses is in agreement with theory. In unstressed material  $4V \rightarrow 1C$  is completely forbidden. High stress reduces the oscillator strength of these resonances again, and at 75 MPa they are no longer detectable. These observations are confirmed in measurements with other frequencies, as represented in Fig. 5. For a smaller frequency ( $\omega_L = 1925.711 \text{ cm}^{-1}$ ), where the structures occur at lower magnetic fields, the shifts of the  $2V \rightarrow 1C$  and  $3V \rightarrow 2C$  resonances and the increase and decrease of the

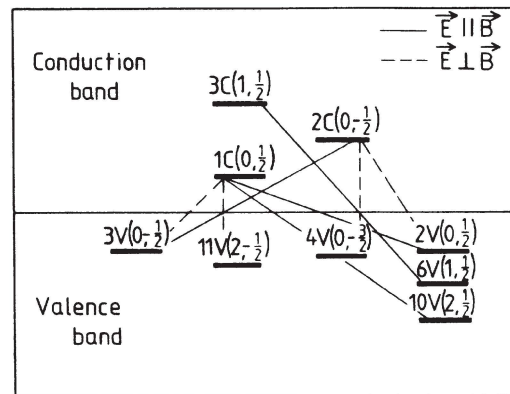


FIG. 6. Classification of the observed energy levels of the conduction band and valence band for  $\mathbf{B} \parallel [001]$  near the band gap. The lines mark identified interband transitions.

$4V \rightarrow 1C$  and  $10V \rightarrow 1C$  intensities have the same stress dependence as discussed.

It should be noticed that the linewidths of the resonances in Figs. 3 and 4 become larger with growing stress. This broadening connected with a diminishing intensity might be due to slightly bending the sample, which causes an inhomogeneous stress in the surface. As the laser focus has a definite size an average of this distribution is measured. In the scheme of Fig. 6 all interband transitions are drawn which have been observed in magnetoreflection. The dashed lines correspond to transitions in polarization  $\mathbf{E} \perp \mathbf{B}$ , the solid lines to  $\mathbf{E} \parallel \mathbf{B}$ .

## V. SUMMARY

Interband transitions in InSb in an external magnetic field have been observed in magnetoreflection. Uniaxial stress modifies both the transition frequencies and the oscillator strengths. Using a magnetic-field-modulation technique numerous transitions were recorded. They could be interpreted as transitions between the valence-band levels 2V, 3V, 4V, 6V, 10V, and 11V and the conduction-band levels 1C, 2C, and 3C. The observed influence of uniaxial stress is in accordance with the theory of paper I. With increasing stress several transitions become observable because the symmetry of the sample is lowered.

\*Present address: Telefunken Electronic, D-7100 Heilbronn, West Germany.

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